

The Expansion History of the Universe: Myths and Facts

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SCIENTIFIC BACKGROUND

- Observations of SNa_e: Interpretation in the Λ CDM model
- Alternative cosmological models: Conformal gravity and kinematic conformal gravity
- GRBs as cosmological probes: Bayesian approach

BAYESIAN ANALYSIS

- Parameter forecasts (posterior probability): Likelihood and priors
- Bayesian evidence: Parallel tempering

High-redshift type Ia Supernovae (SNaE)



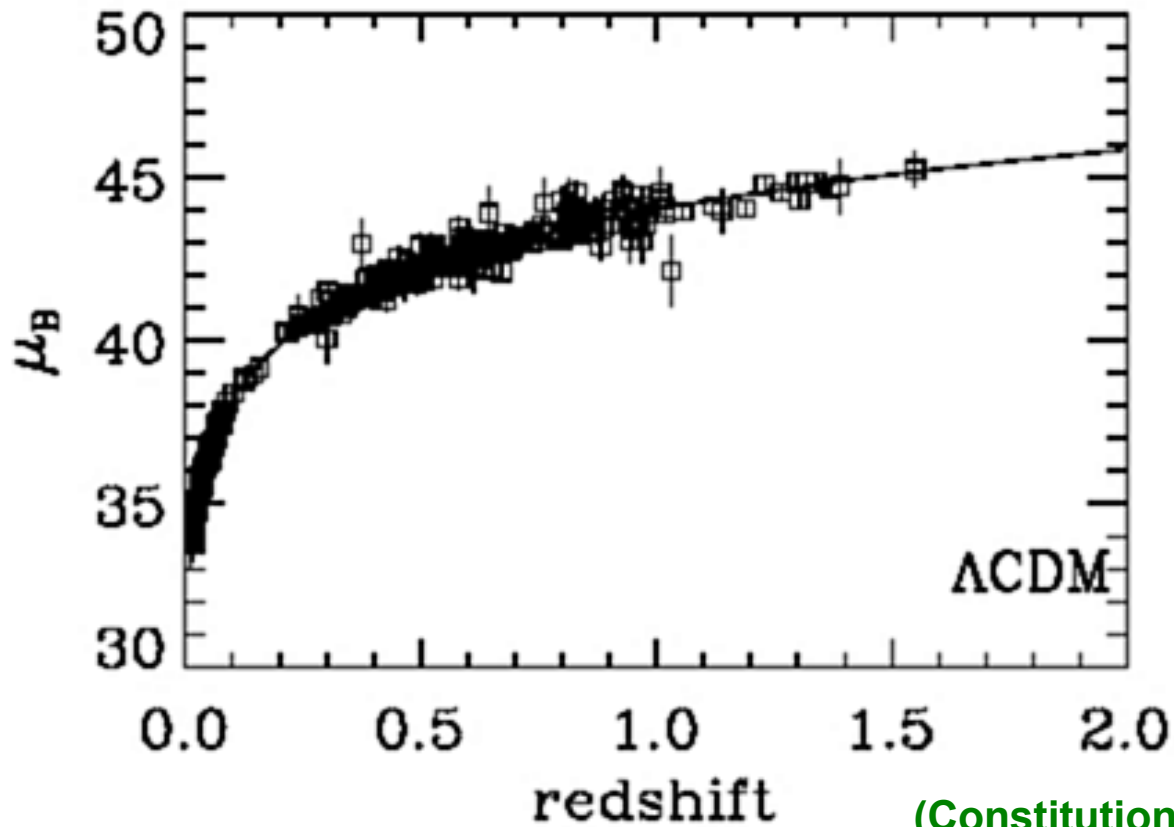
Hubble Diagram of SNaE in Λ CDM

$$\mu_B(\theta, z_i) \approx m_i - M = 5 \log_{10} d_L(\theta, z) - 5$$

Cosmological parameters Ω_0 (and Ω_Λ)

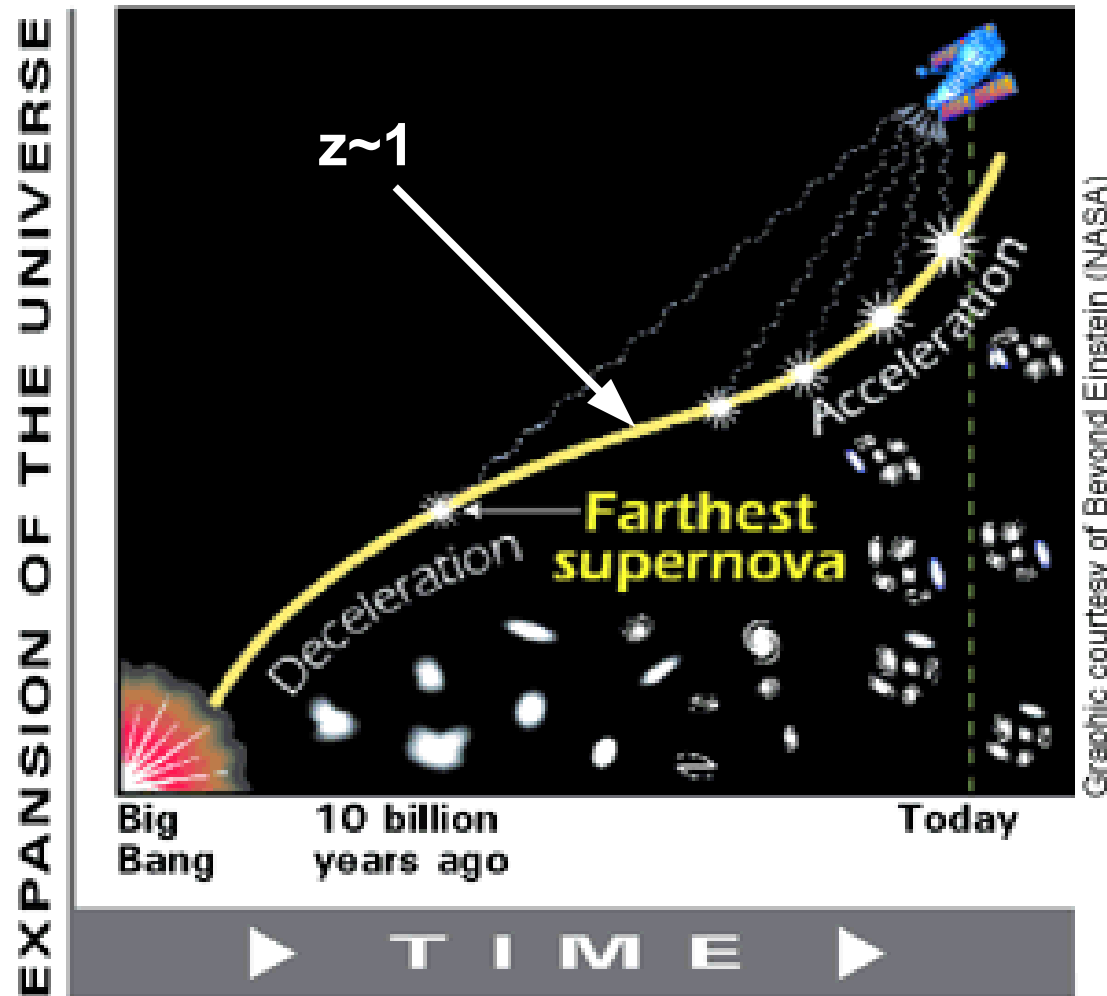
Observables

Intrinsic luminosity



(Constitution set of Hicken et al 2009)

The expansion history of the Λ CDM model



Can we probe the deceleration phase at redshift larger than $z \approx 1$?

Conformal gravity: No deceleration phase!

- Conformal cosmology (CG) (Mannheim 1990)
- Kinematic conformal cosmology (KCG) (Varieschi 2010)

Cosmology in conformal gravity - CG

Action:

$$I_W = -\alpha \int d^4 x \sqrt{-g} C_{\mu\nu\kappa\lambda} C^{\mu\nu\kappa\lambda} \quad g_{\mu\nu}(x) \Rightarrow \Omega(x) g_{\mu\nu}(x)$$

“Friedmann” equation:

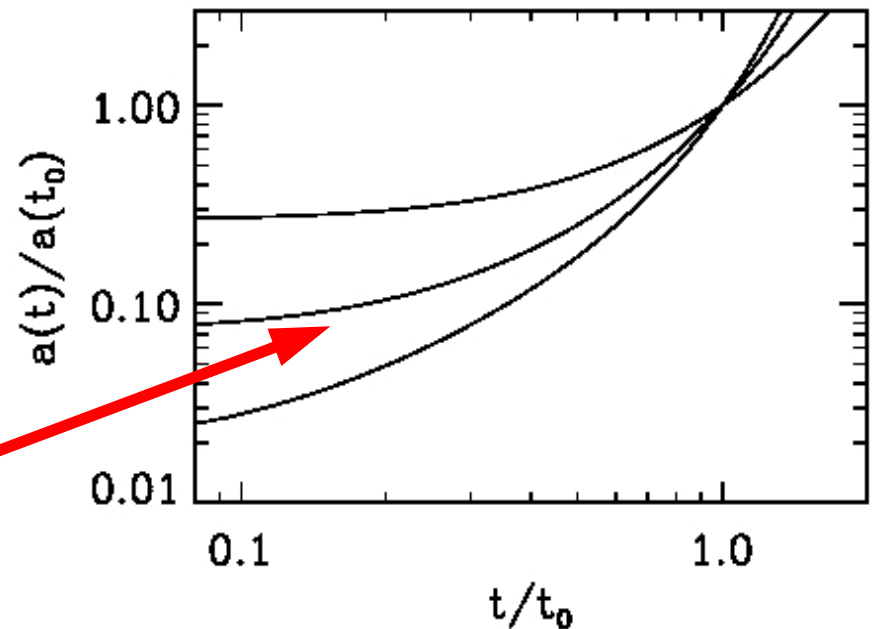
$$\dot{a}^2 a^2 = H_0^2 (\Theta_\Lambda a^4 + \Theta_k a^2 - \Theta_{nr} a - \Theta_r)$$

Deceleration parameter:

$$q = -\frac{\Theta_{nr}}{2} - \Theta_r - \Theta_\Lambda$$

(Same as Λ CDM model
with $\Theta_{nr,r} \rightarrow -\Omega_{nr,r}$)

Always accelerated expansion!



Kinematic conformal cosmology - KCG

Conformal gravity Schwarzschild solution:

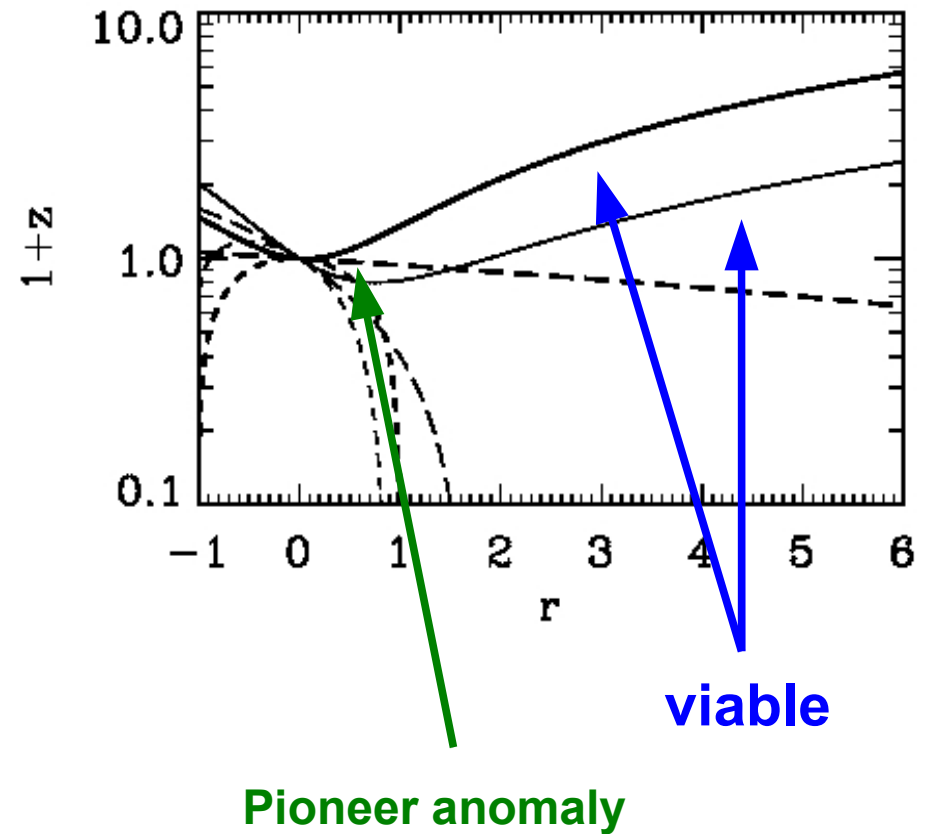
$$ds^2 = -B(r) c^2 dt^2 + \frac{dr^2}{B(r)} + r^2 d\Omega \quad \text{with } B(r) = 1 - \frac{\beta(2-3\beta\gamma)}{r} - 3\beta\gamma + \gamma r - \kappa r^2$$

Redshift

$$1+z = \frac{a(0)}{a(r)} = \sqrt{1 - kr^2} - r\delta$$

New inverse-square law:

$$F(d_L) = \frac{L_0}{4\pi d_L^2} \left(\frac{d_{rs}}{d_L} \right)^{a_v}$$



Distance modulus

Λ CDM and CG

$$\mu(\theta, z) = 5 \log_{10} d_L(\theta, z) - 5$$

$$\theta = \begin{cases} \Omega_0 & \Lambda \text{CDM} \\ q_0 & \text{CG} \end{cases}$$

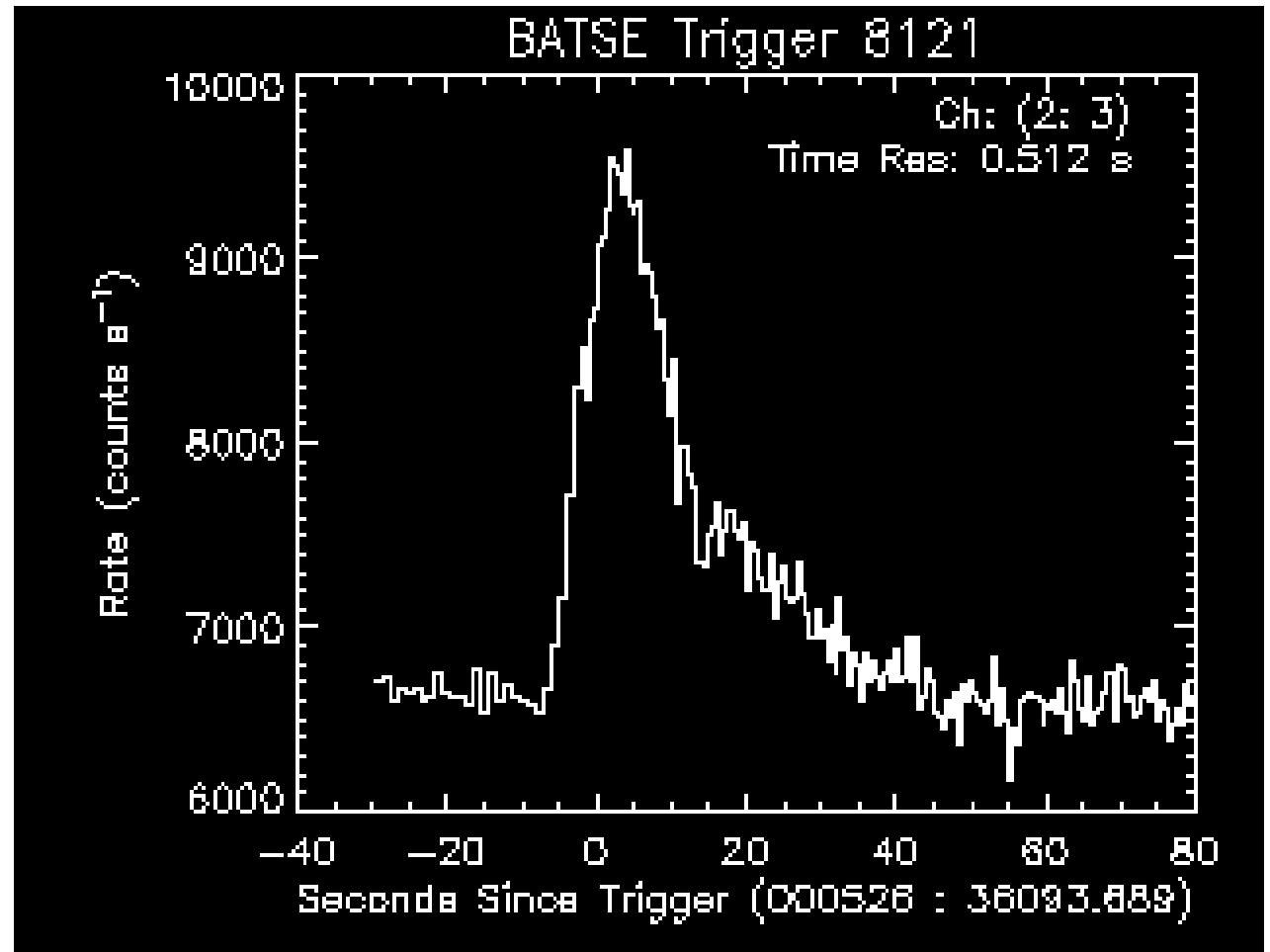
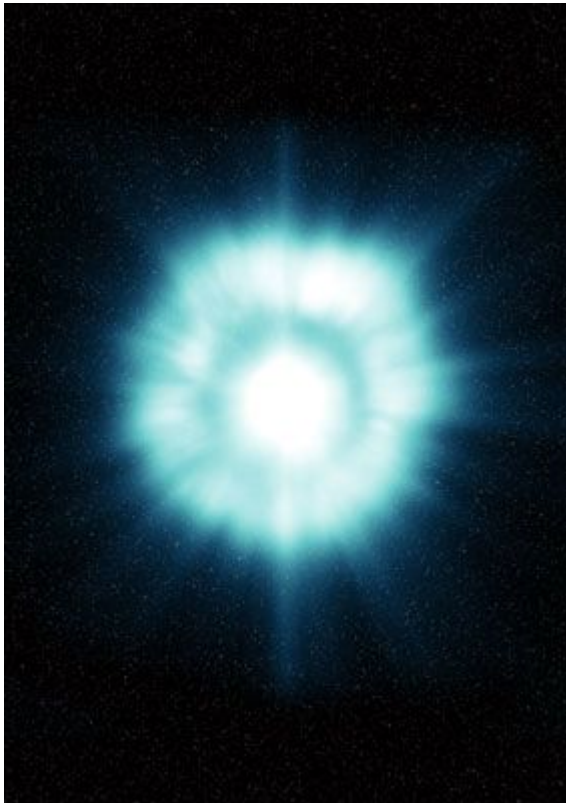
KCG

$$\mu(\theta, z) = 2.5(2 + a_V) \log_{10} \left[\frac{\delta_0(1+z) + \sqrt{(1+z)^2 - (1 - \delta_0^2)}}{2\delta_0} \right]$$

$$\theta = (a_V, \delta_0)$$

Gamma-ray bursts (GRBs) as cosmological probes

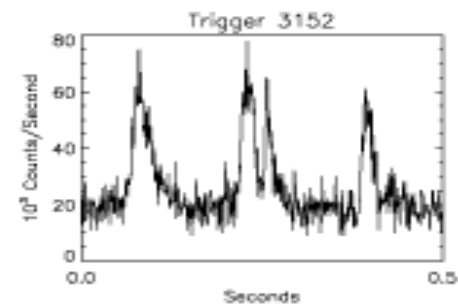
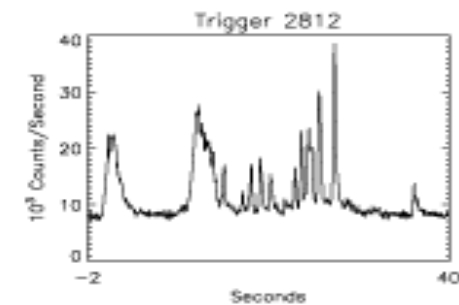
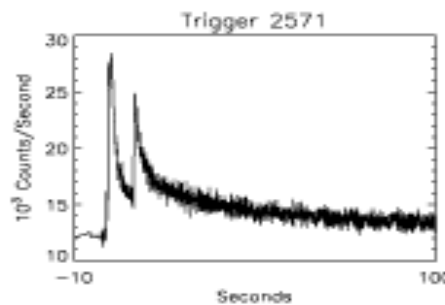
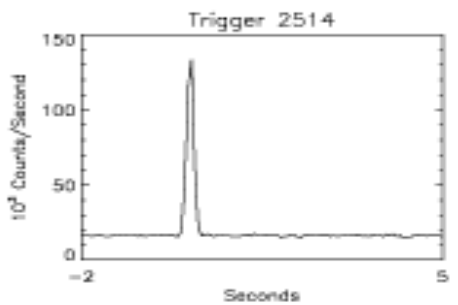
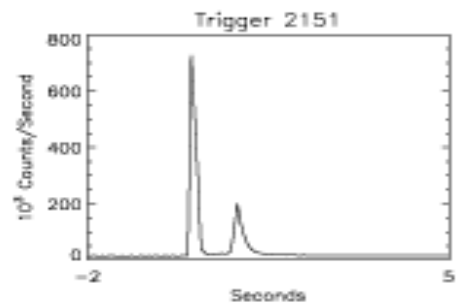
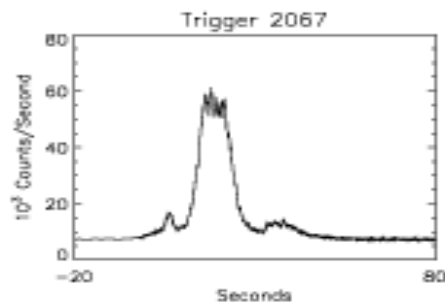
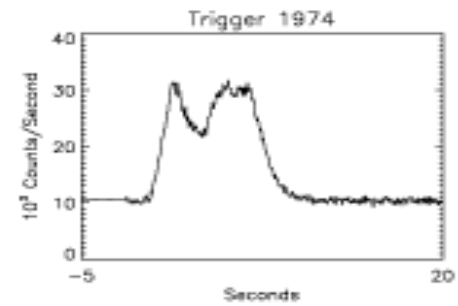
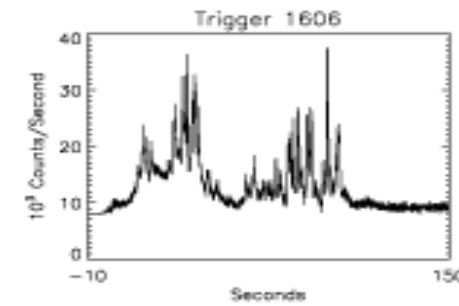
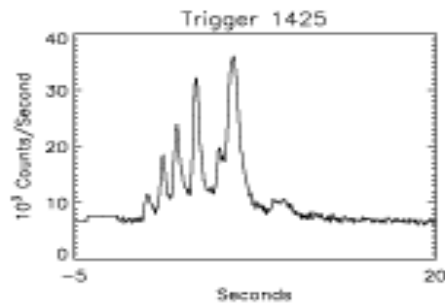
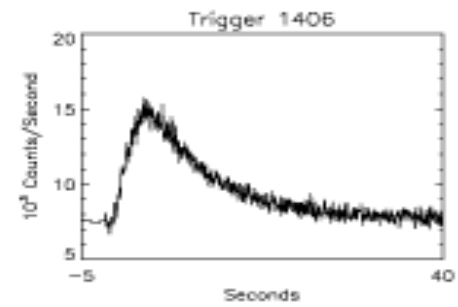
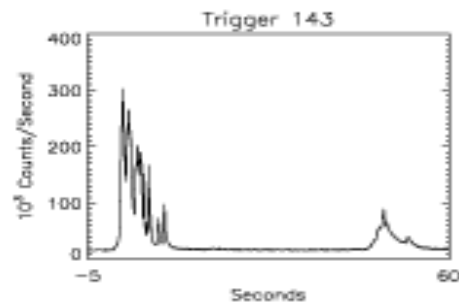
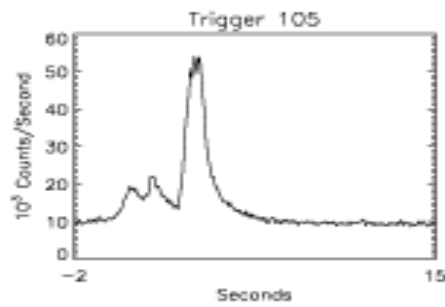
Light curve



GRBs are currently observed up to redshift $z \sim 8$

GRB light curves

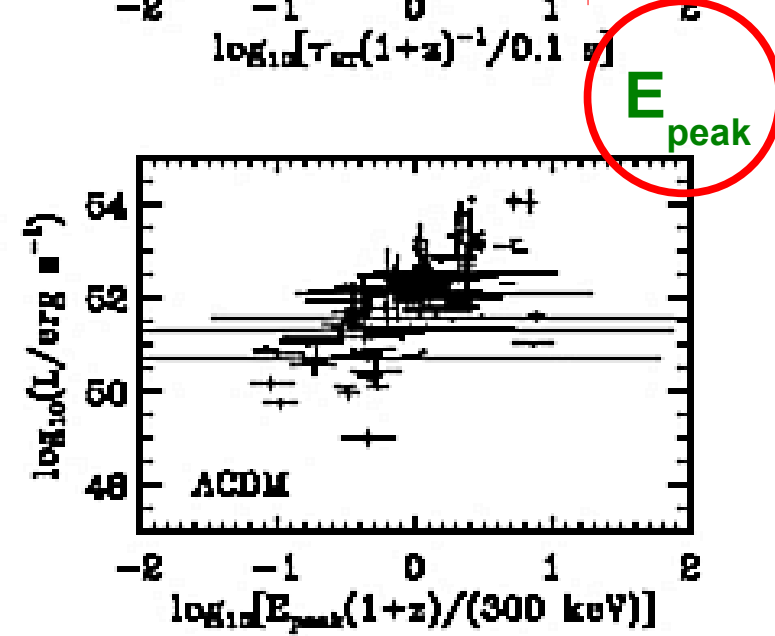
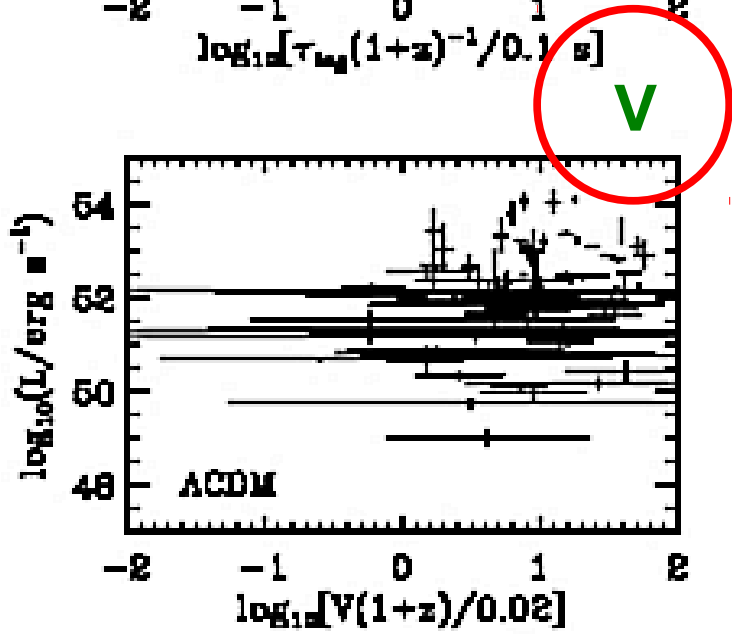
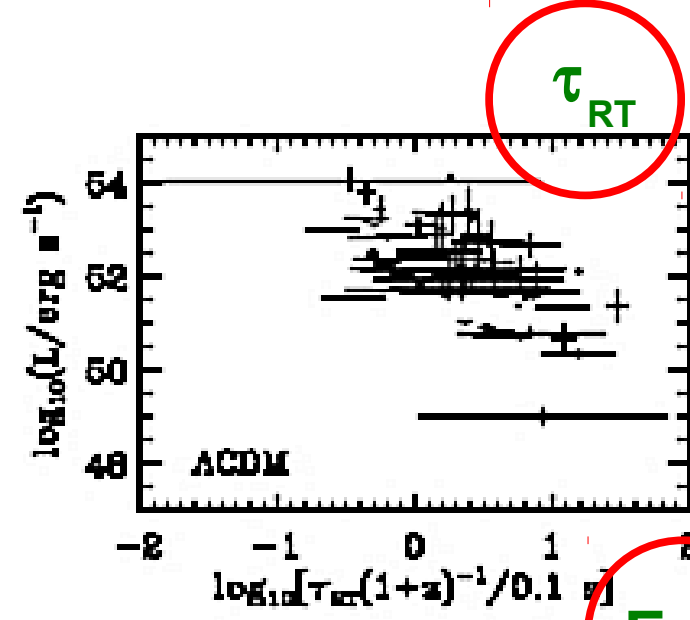
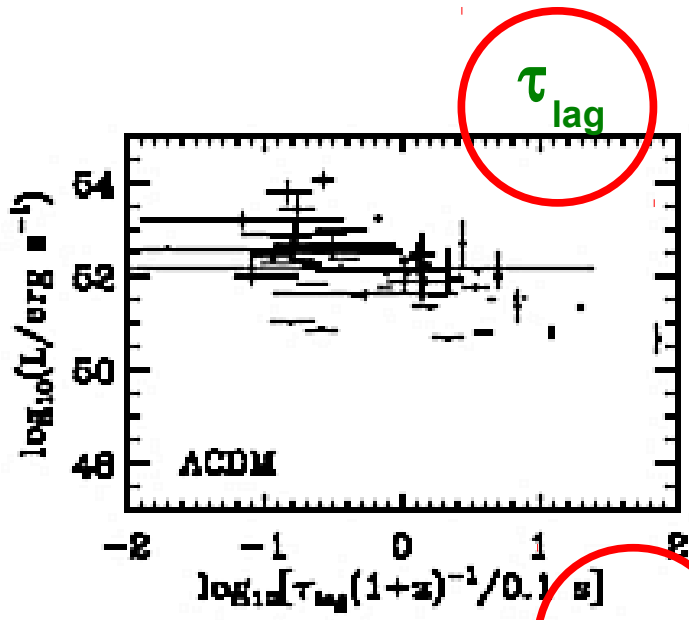
Counts/second



Time

GRB distance indicators

Luminosity



Light-curve parameter

(GRB sample from Schaefer 2007)

Distance indicator relations

$$\log_{10} P_{\text{bolo}} = a + b \log_{10} X - f(\theta, z)$$

X = light-curve parameter

flux

$$f(\theta, z) = \log_{10}[4\pi d_L^2(\theta, z)] \quad (\Lambda\text{CDM, CG})$$

$$f(\theta, z) = \log_{10}[4\pi d_L^2(\theta, z)] + a_V \log_{10}\left(\frac{d_L}{d_{rs}}\right) \quad (\text{KCG})$$

NO NEARBY GRBs → NO CALIBRATION (unlike SNaE)

Bayesian parameter estimation

$$p(\theta|D, M) = \frac{p(D|\theta, M) p(\theta|M)}{p(D|M)}$$

Likelihood

$$p(D|\theta, M) \sim \exp\left(-\frac{1}{2} \delta Y^T C^{-1} \delta Y\right)$$

$\delta Y = \text{measures} - \text{expected values}(\theta)$

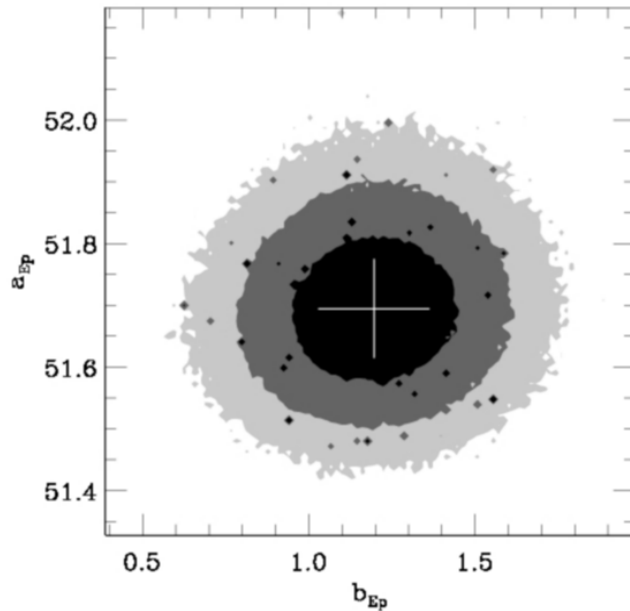
$D = \{\text{all the observables, including uncertainties}\}$

$C = \text{covariance matrix}$

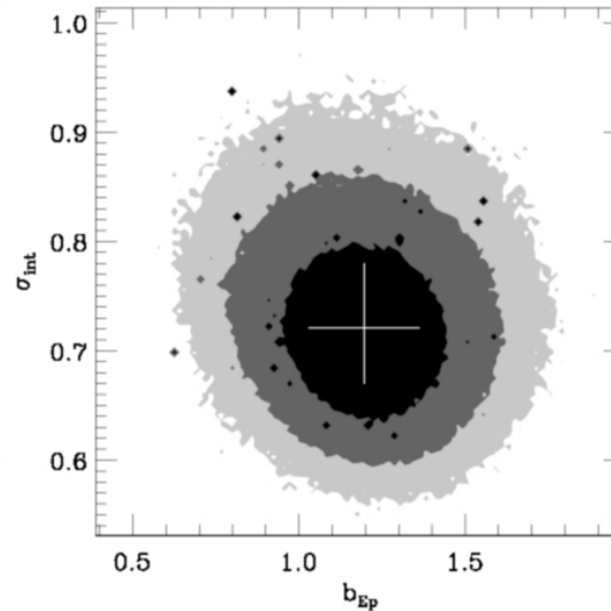
Analysis is performed over the 4 relations at the same time!

Parameter probability density functions: $p(\theta | D, M)$

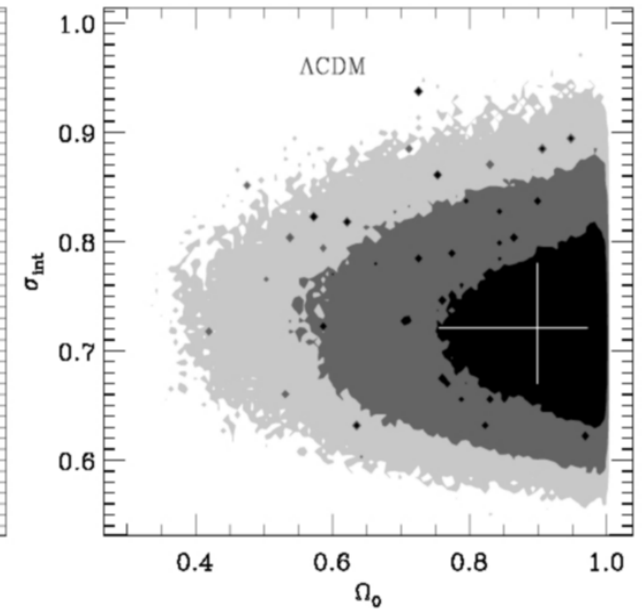
a vs b



σ_{int} vs b



σ_{int} vs Ω_0



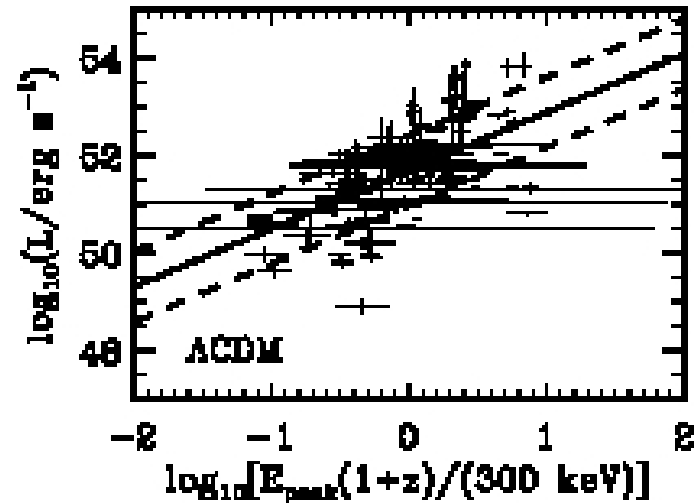
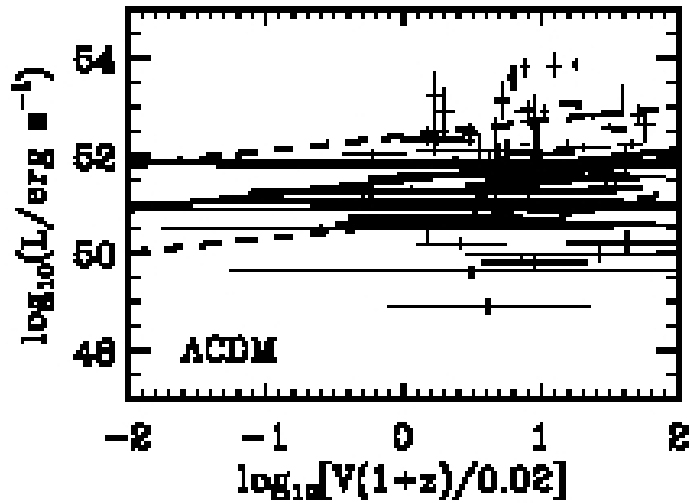
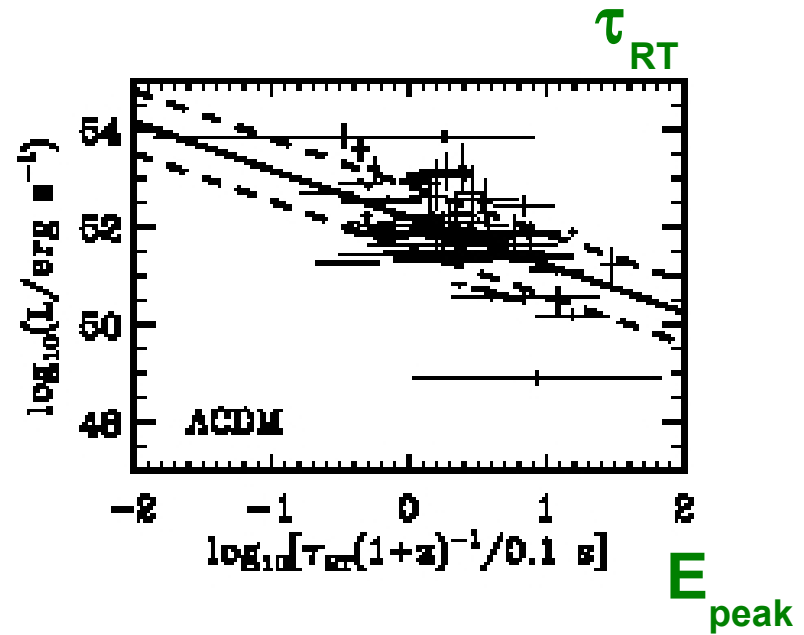
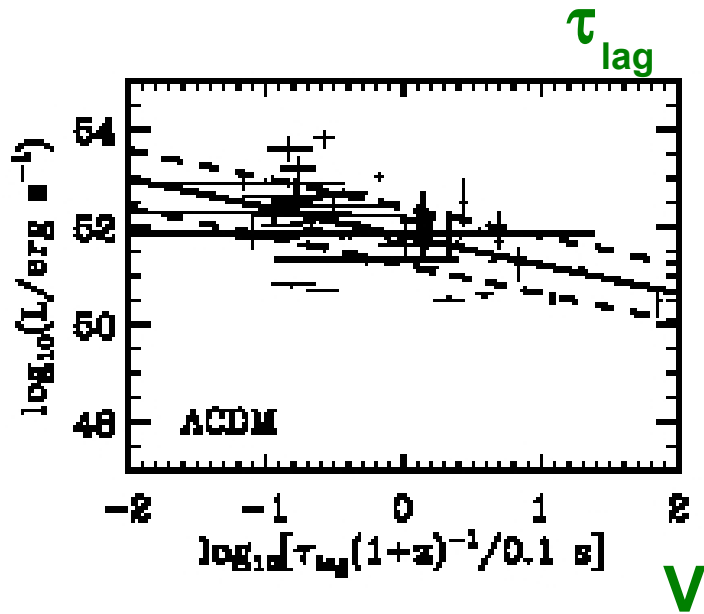
(similar PDFs for the 4 relations)

$$\log_{10} P_{bolo} = a + b \log_{10} X - f(\theta, z)$$

$W_i = a + b \log_{10} X_i - f(\theta, z_i)$ is the mean of $\log_{10} P_{bolo}^i$ with variance σ_{int}^2

GRBs distance indicators

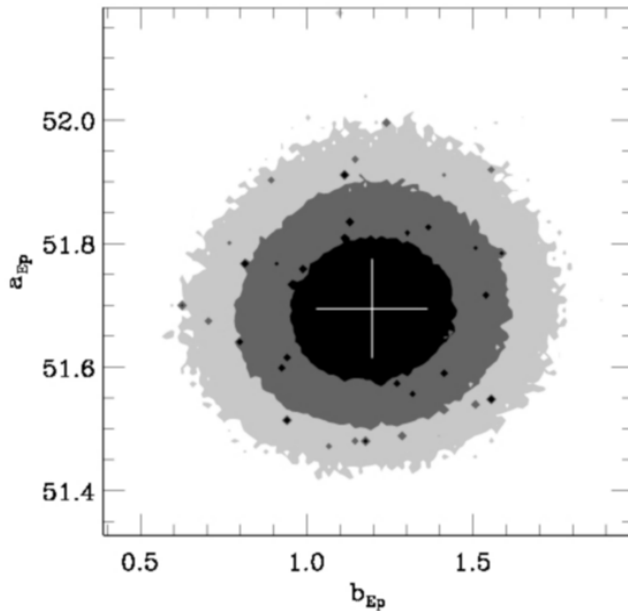
Luminosity



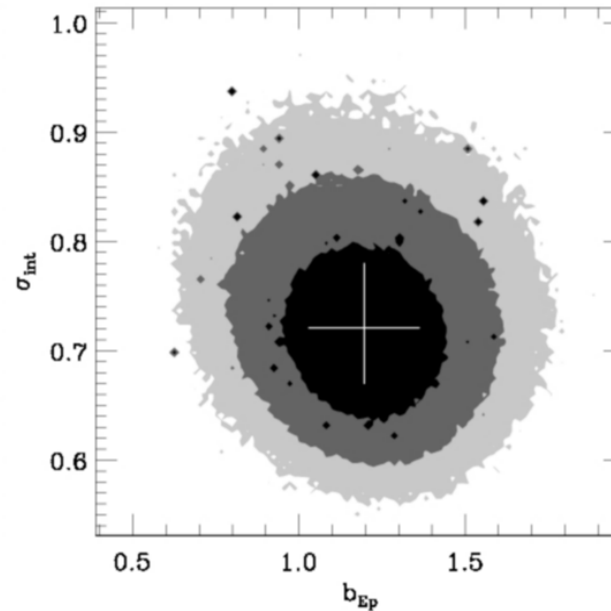
Light-curve parameter

Parameter probability density functions: $p(\theta | D, M)$

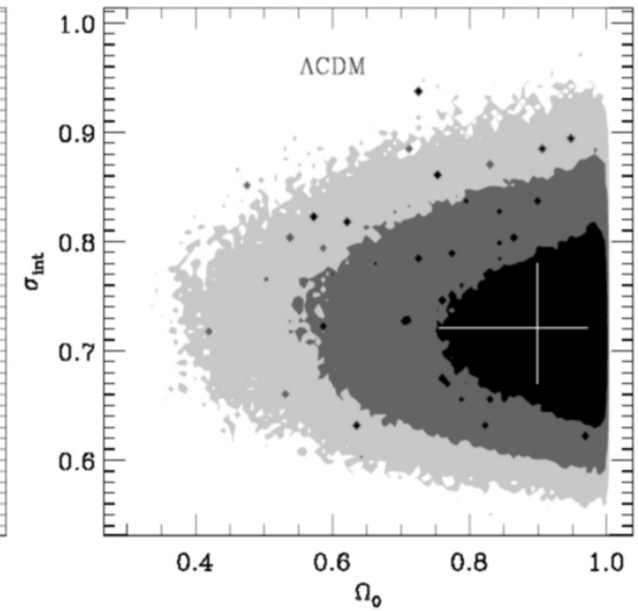
a vs b



σ_{int} vs b



σ_{int} vs Ω_0

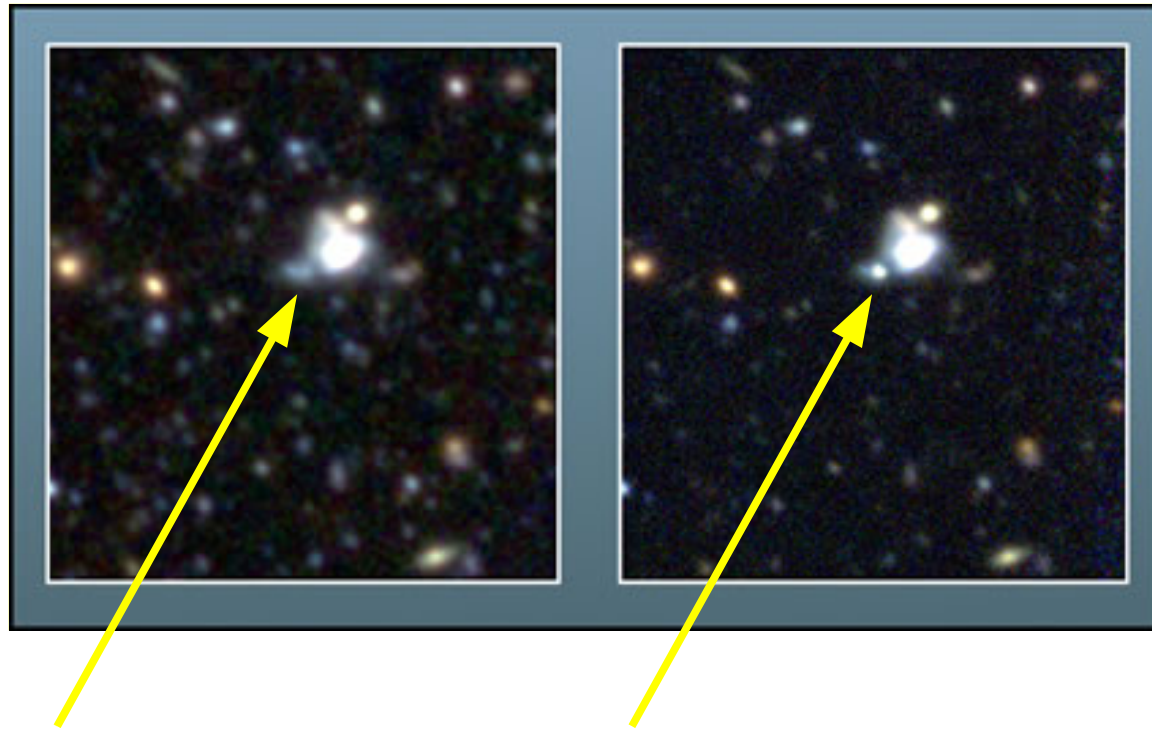


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$$\log_{10} P_{bolo} = a + b \log_{10} X - f(\theta, z)$$

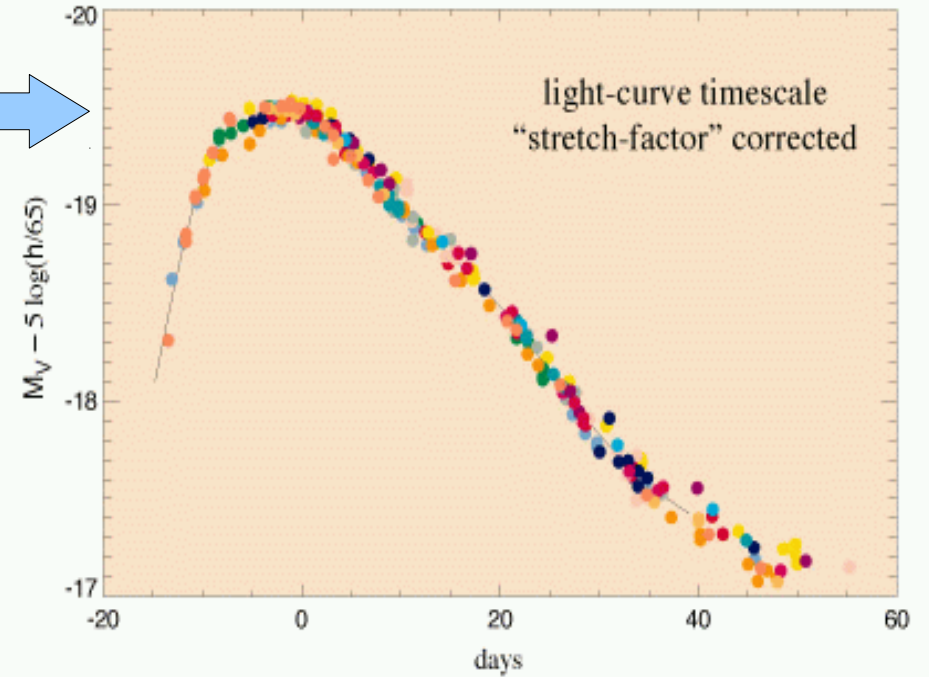
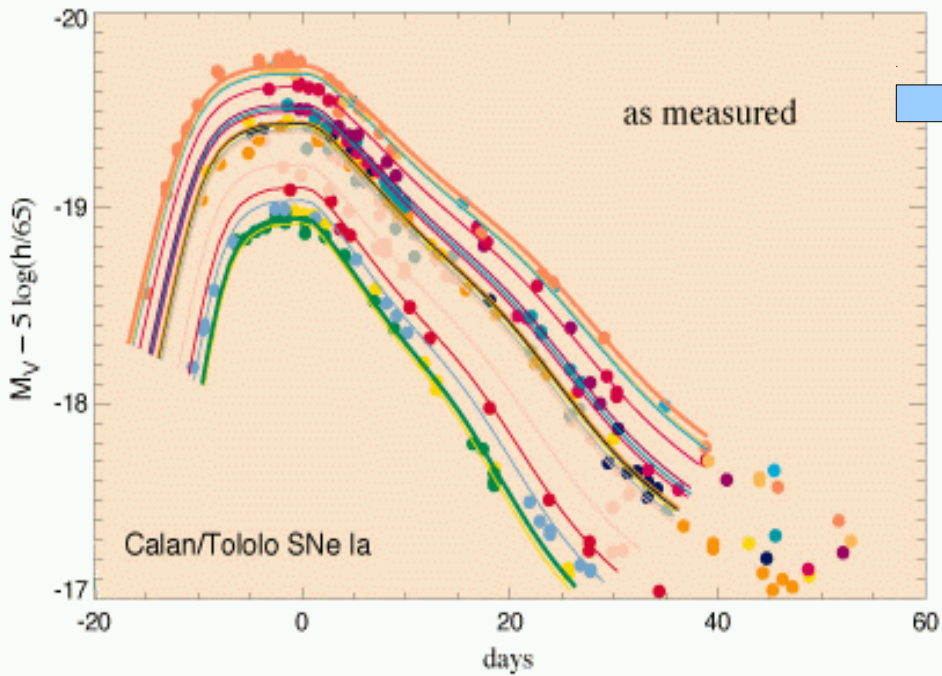
$W_i = a + b \log_{10} X_i - f(\theta, z_i)$ is the mean of $\log_{10} P_{bolo}^i$ with variance σ_{int}^2

Combining with other probes to obtain tighter constraints?
e.g. SNaE



Supernova Light Curves

V Band



Shape parameter

Colour parameter

$$\mu_B(\theta, z_i) = m_i - M + \alpha(s_i - 1) - \beta c_i$$

Cosmological parameters

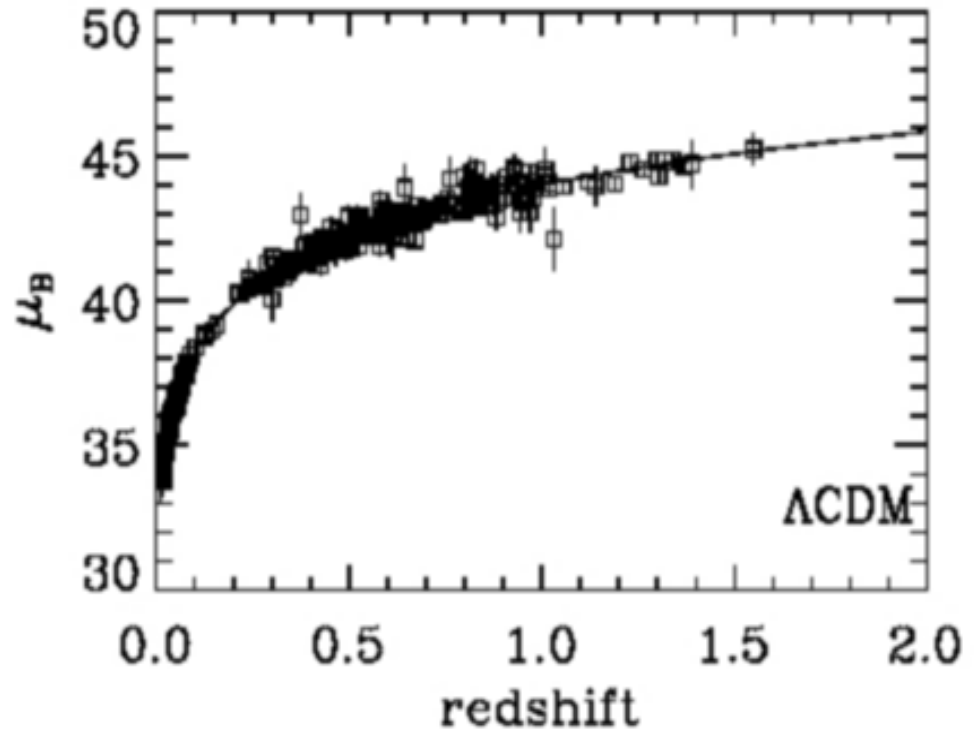
Free parameters

Observed and derived quantities

$$\mu_B(\theta, z_i) = m_i - M + \alpha(s_i - 1) - \beta c_i$$

Observables

This is NOT a plot of directly observed quantities!

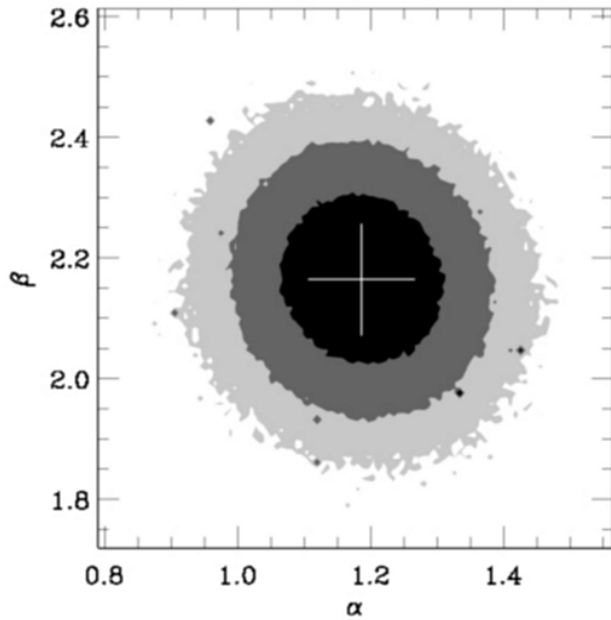


(Constitution set of Hicken et al 2009)

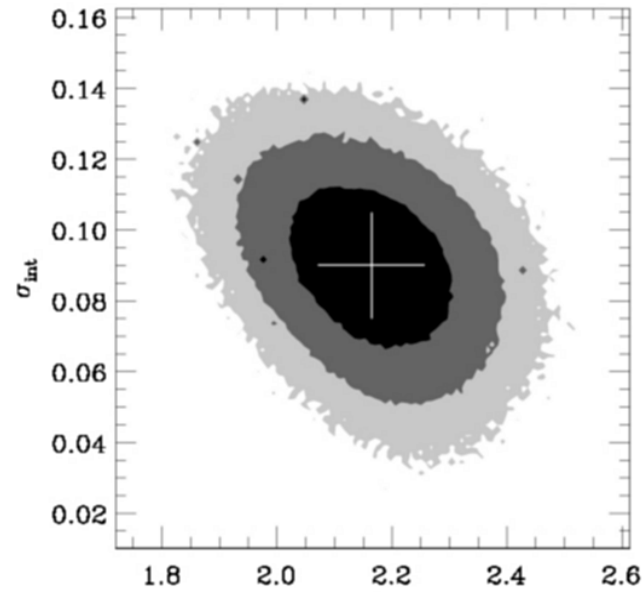
Bayesian parameter estimation again...

Parameter probability density functions: $p(\theta | D, M)$ derived for the SNae alone

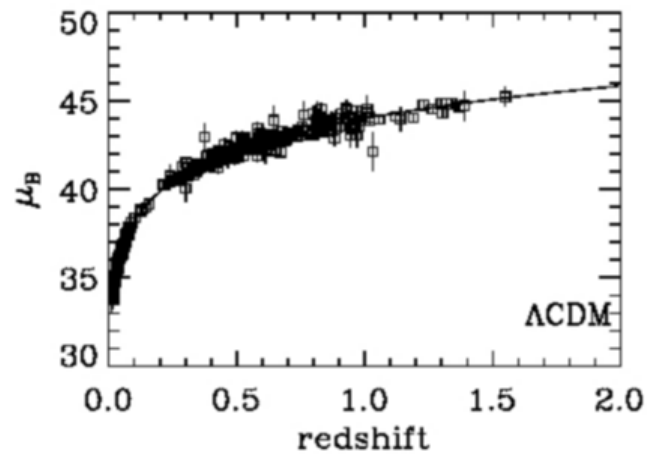
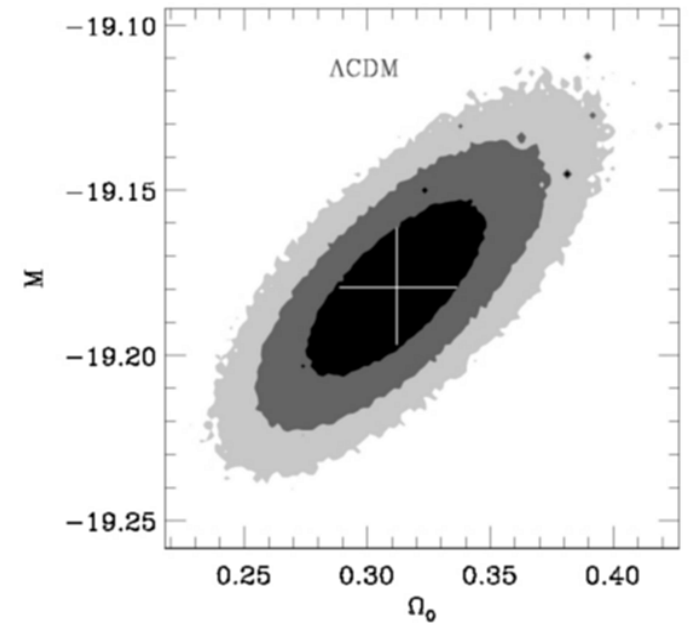
β vs α



σ_{int} vs β



M vs Ω_0



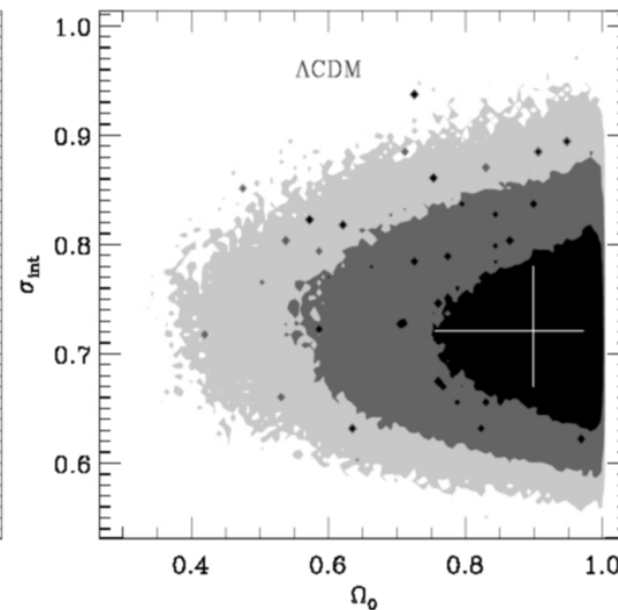
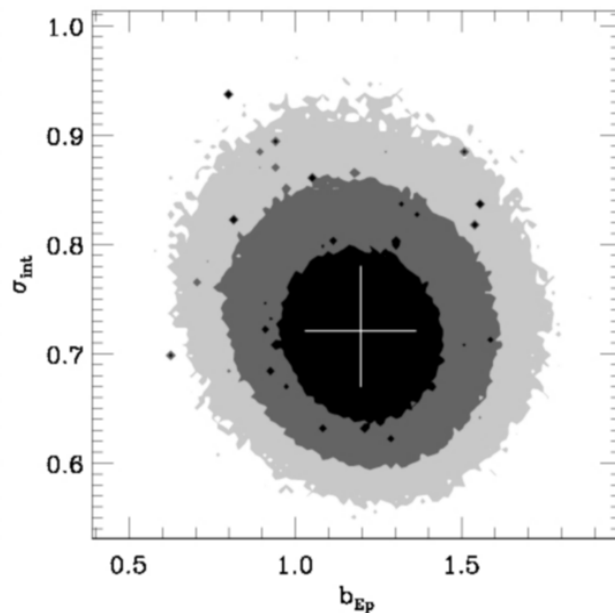
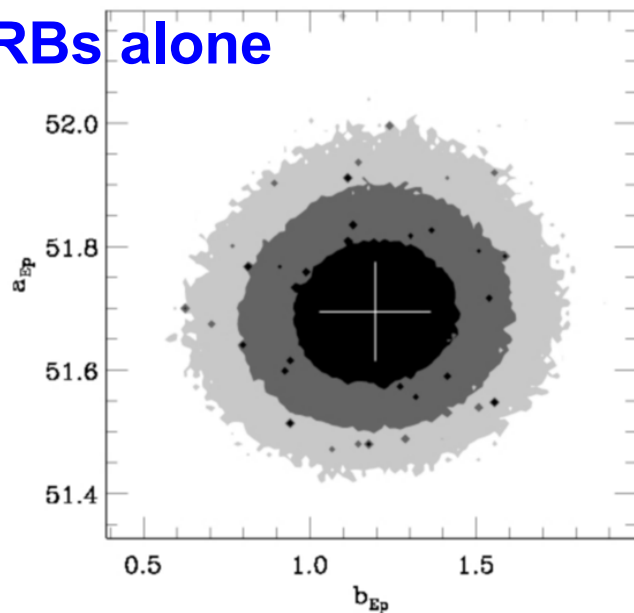
Combining GRBs with SNaE

a vs b

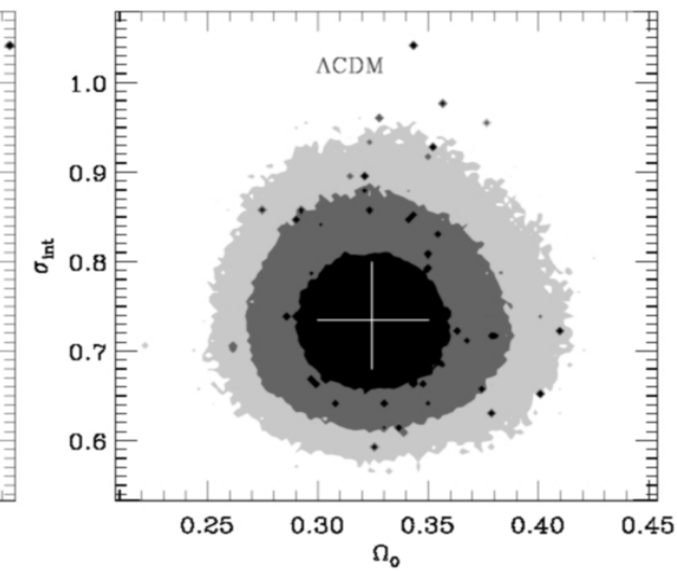
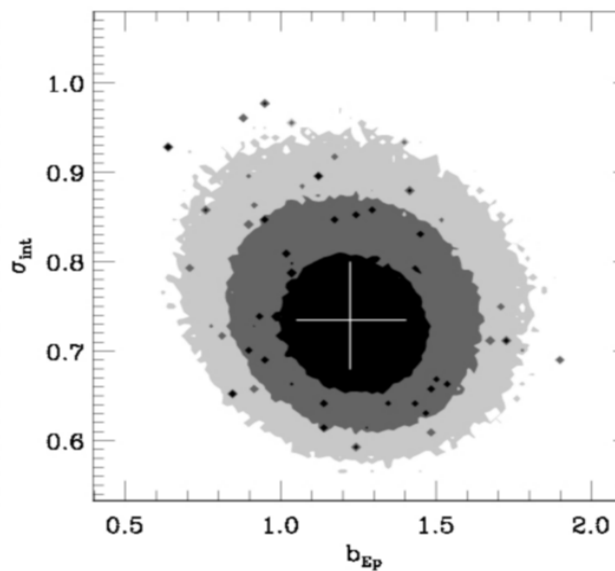
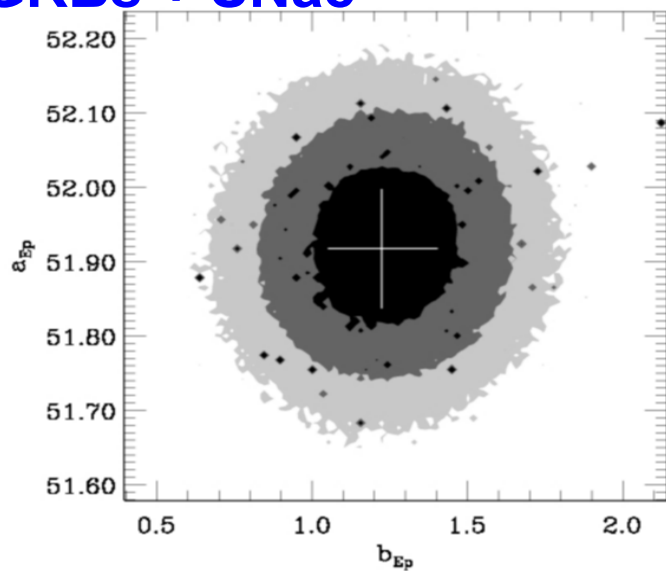
σ_{int} vs b

σ_{int} vs Ω_0

GRBs alone



GRBs + SNaE



What happens in CG and KCG?

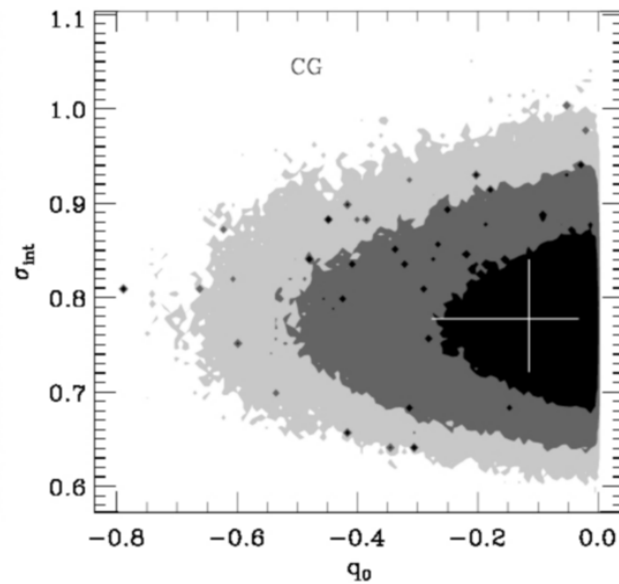
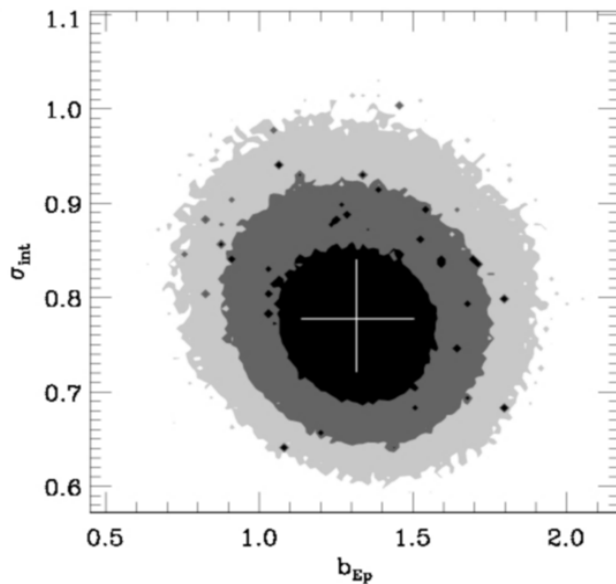
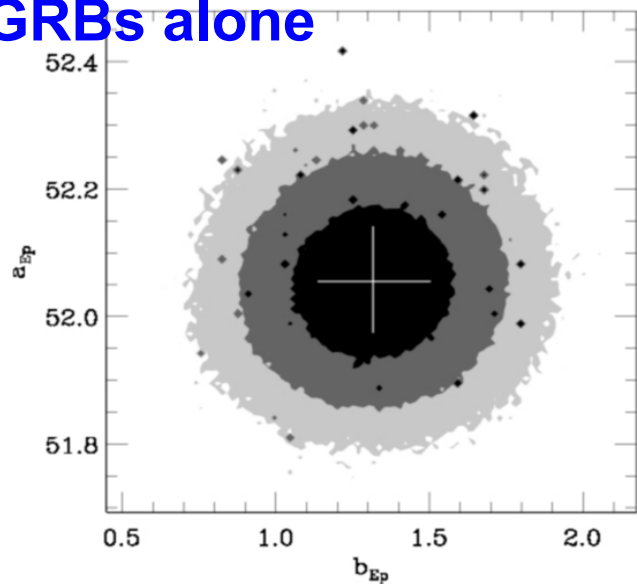
CG

a vs b

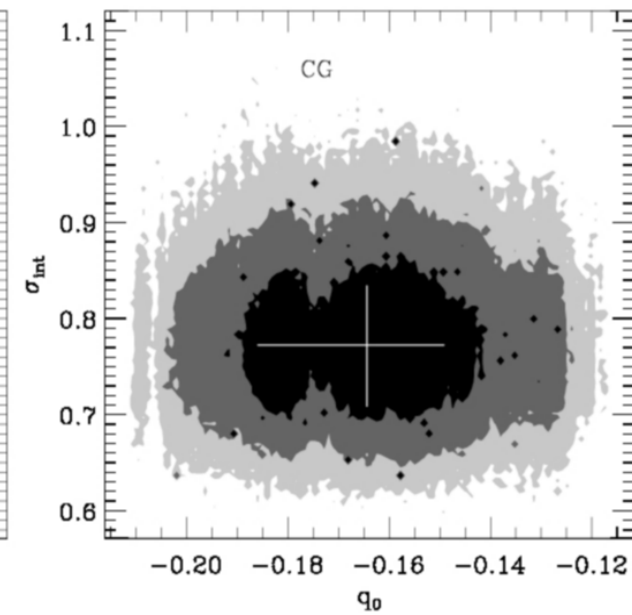
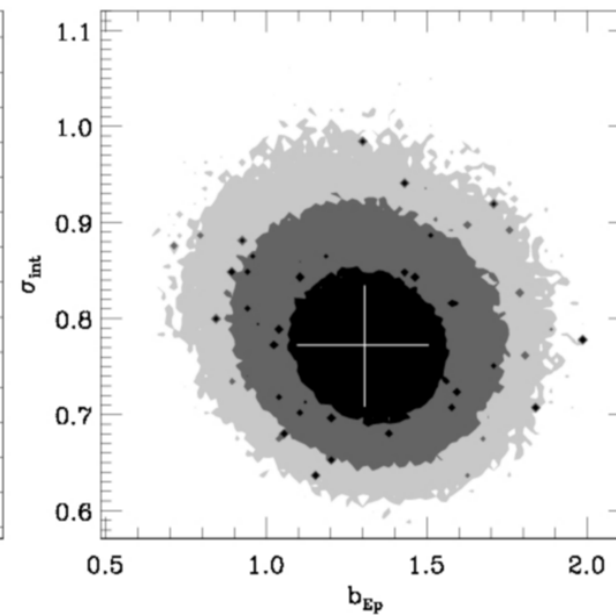
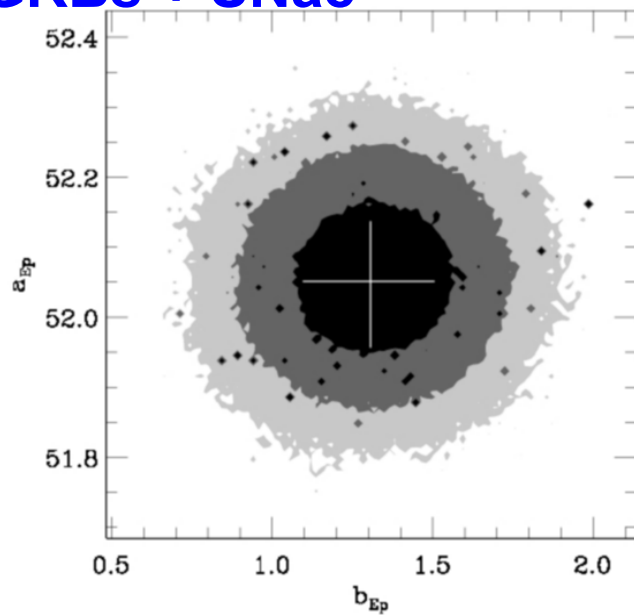
σ_{int} vs b

σ_{int} vs q_0

GRBs alone



GRBs + SNaE



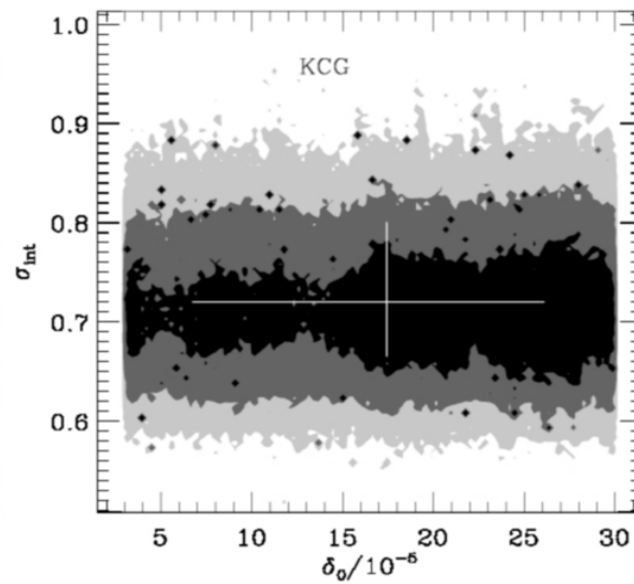
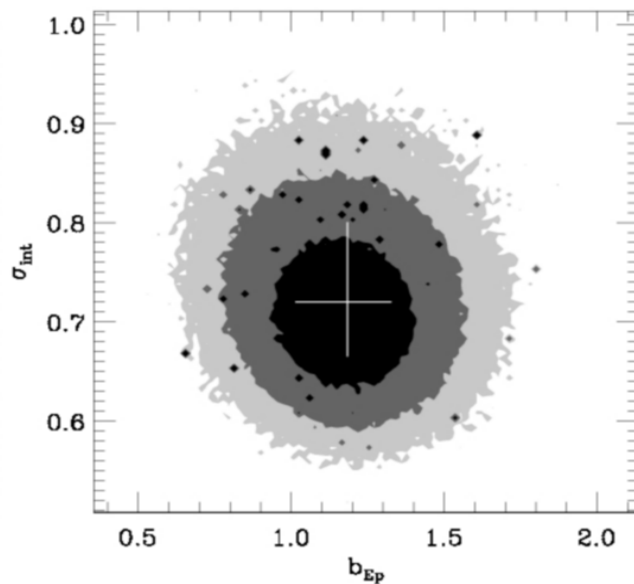
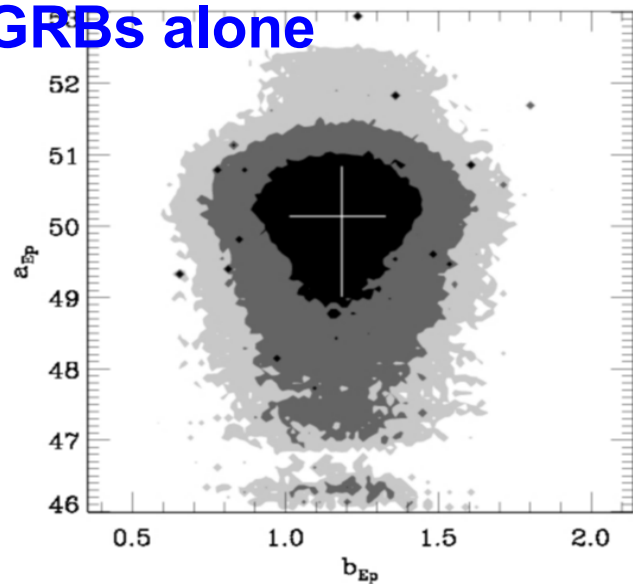
KCG

a vs b

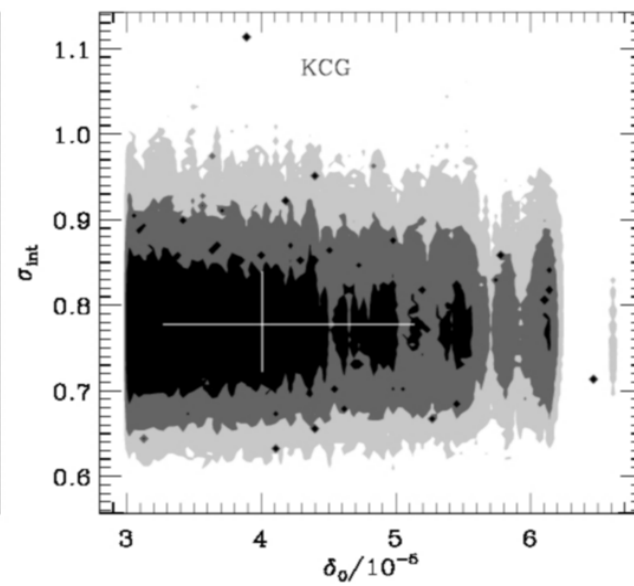
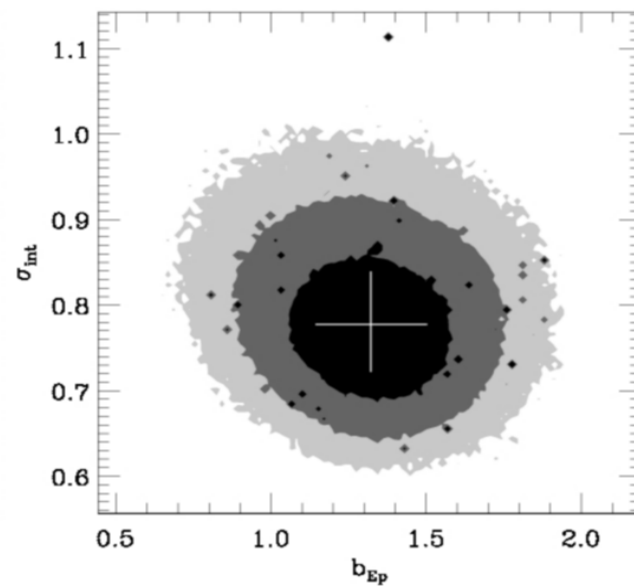
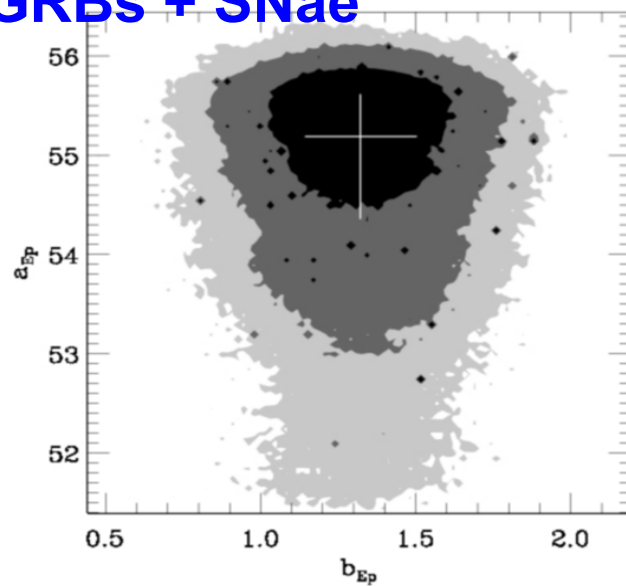
σ_{int} vs b

σ_{int} vs δ_0

GRBs alone

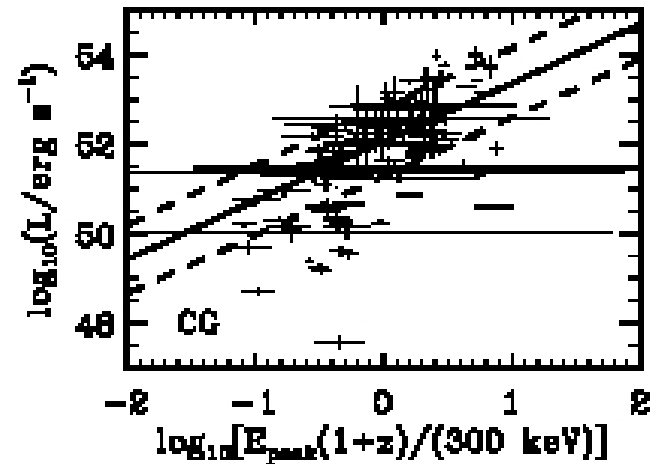
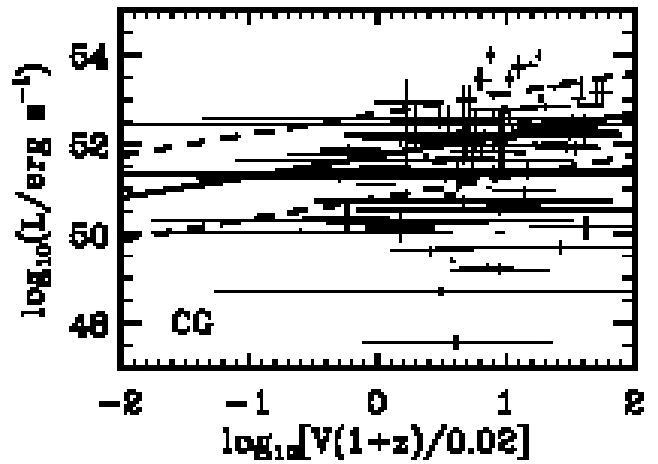
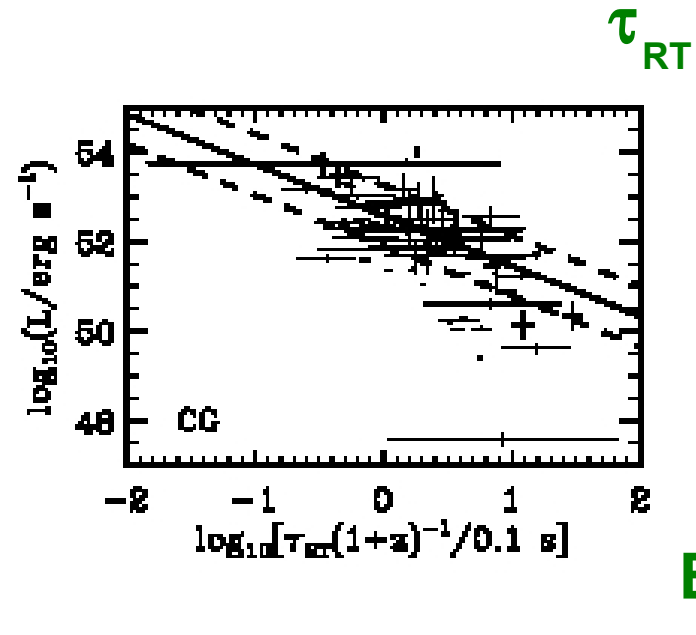
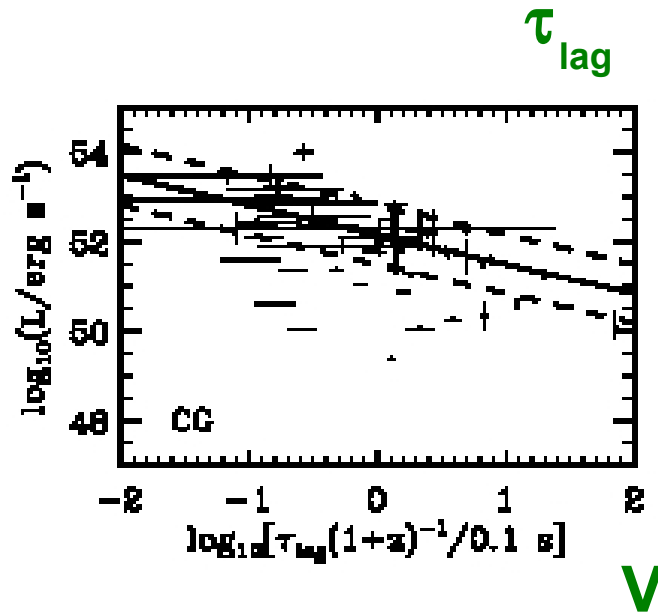


GRBs + SNaE



GRBs distance indicators in CG

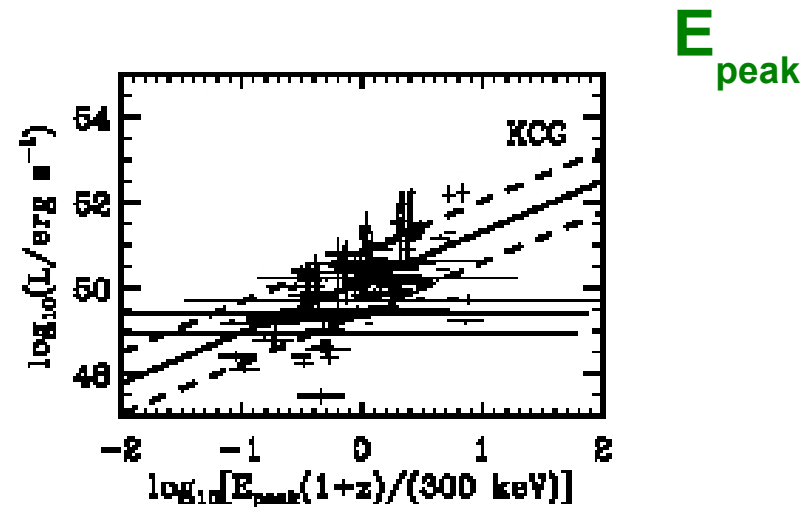
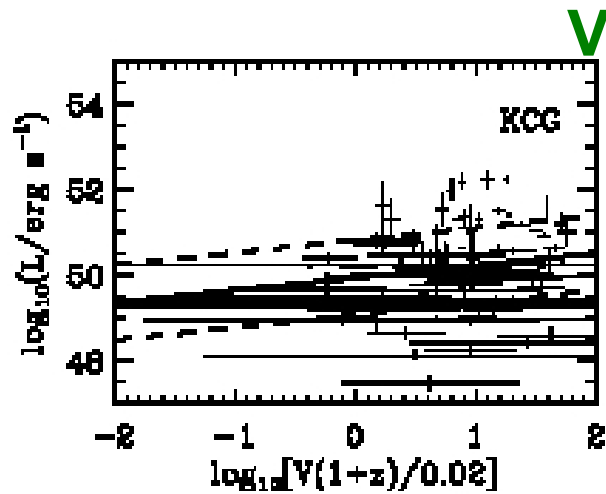
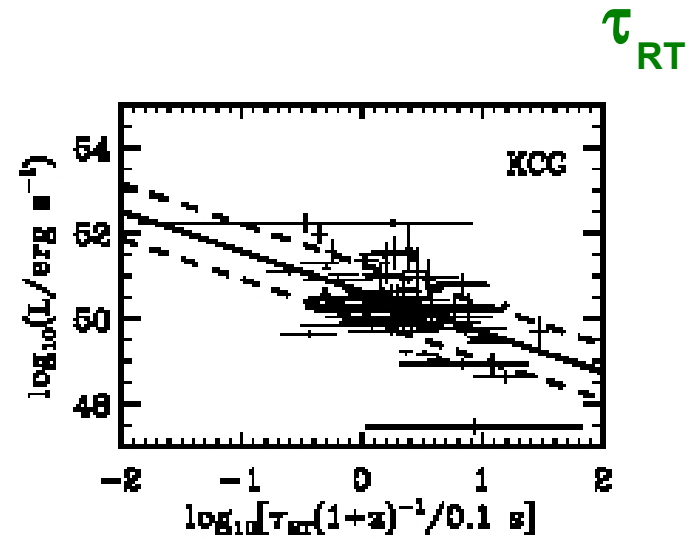
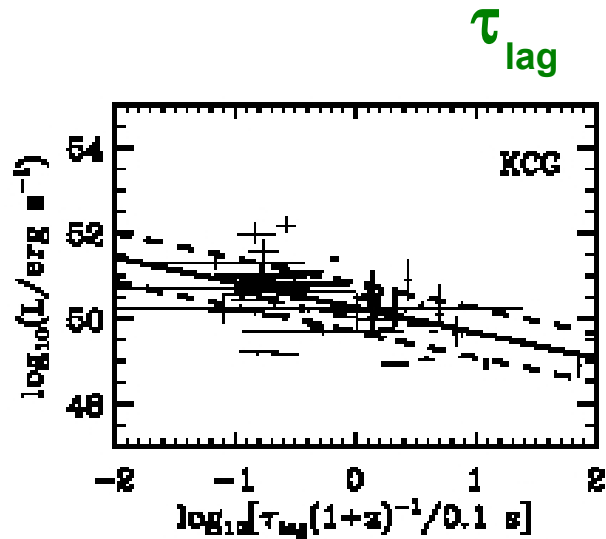
Luminosity



Light-curve parameter

GRBs distance indicators in KCG

Luminosity



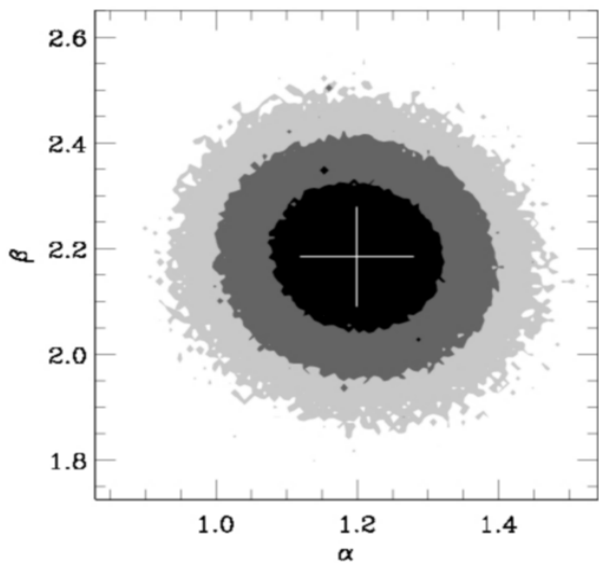
Light-curve parameter

**Models without an early decelerated expansion
can clearly describe the GRB data**

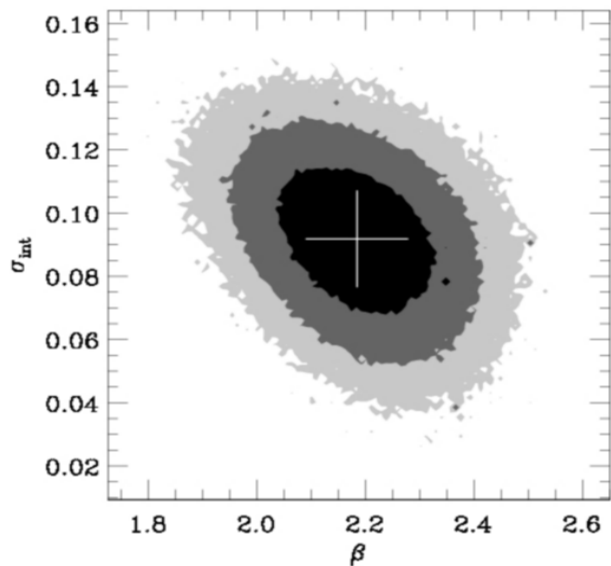
For completeness: SNae in CG and KCG?

PDFs of SNaE parameters in CG

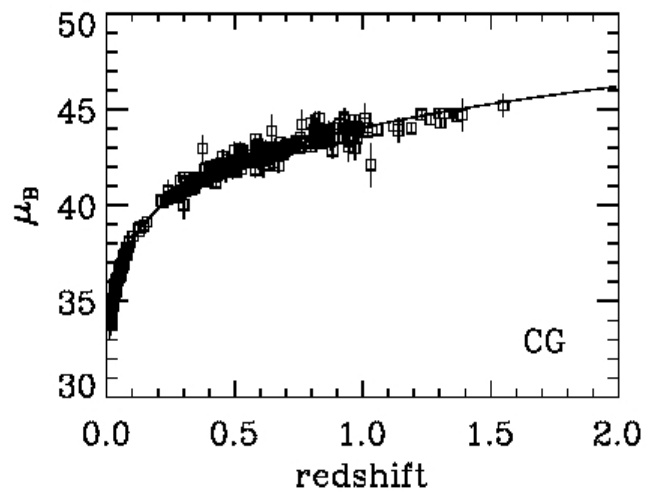
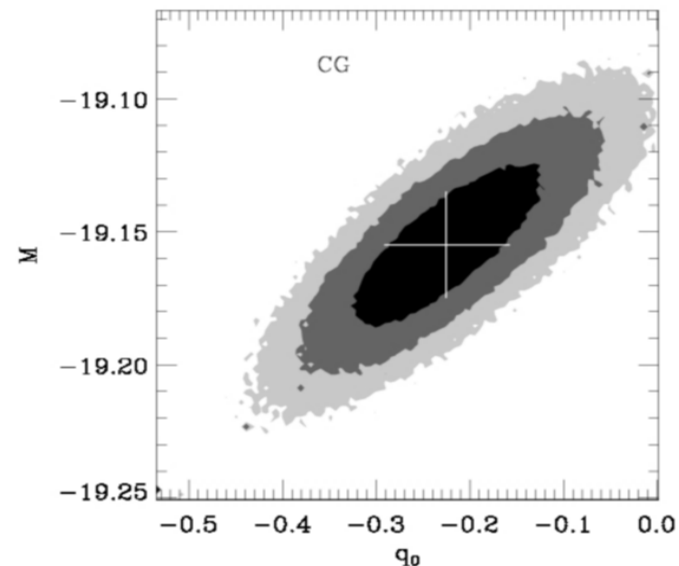
β vs α



σ_{int} vs β

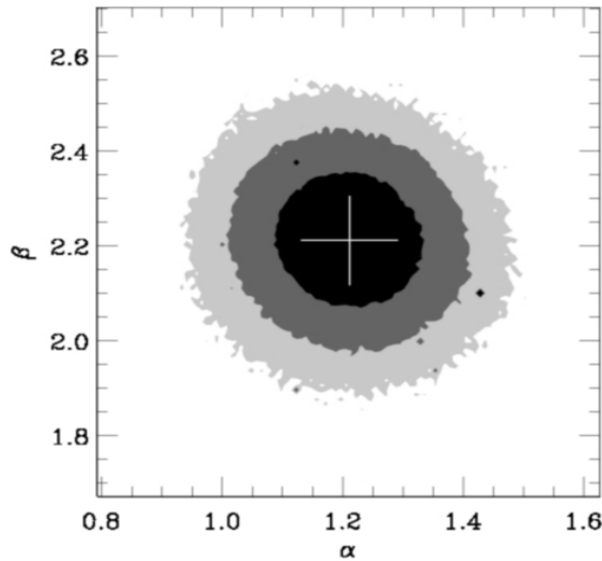


M vs q_0

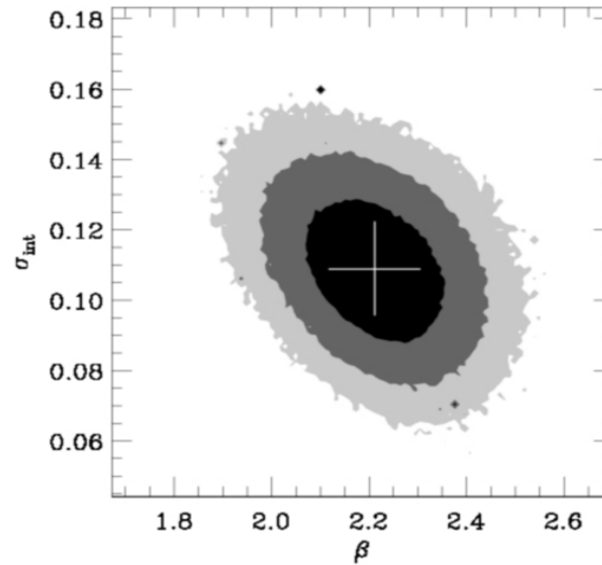


PDFs of SNae parameters in KCG

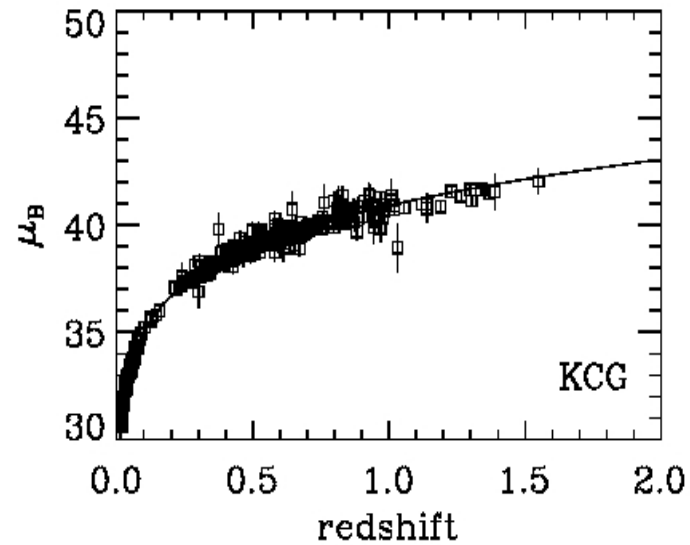
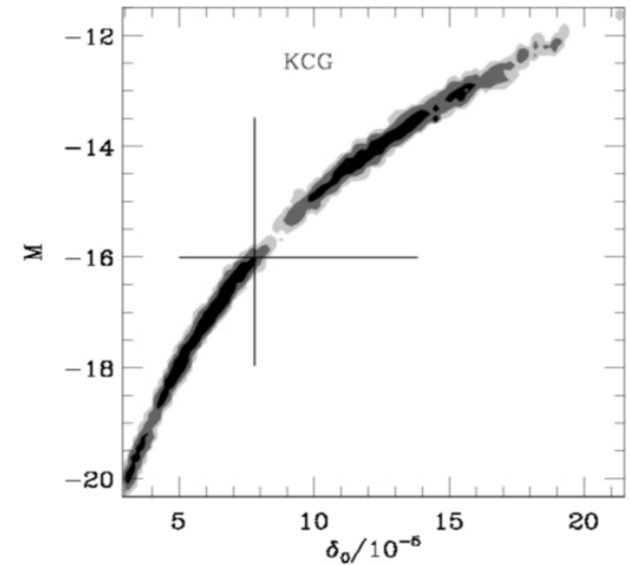
β vs α



σ_{int} vs β

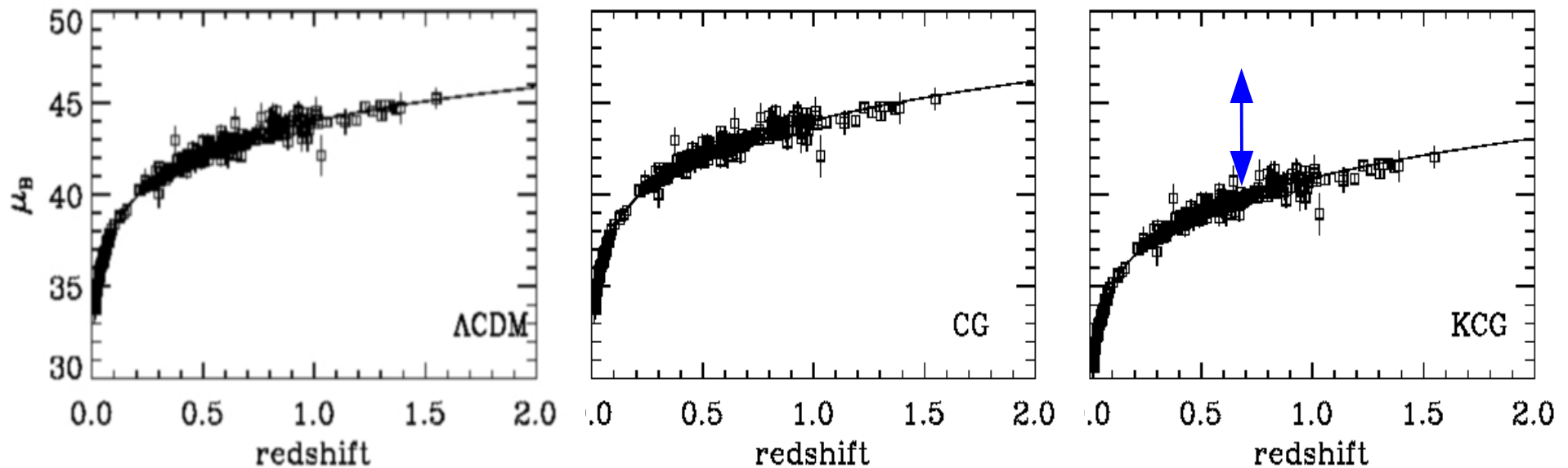


M vs δ_0



Hubble diagram of SNaE in the three models

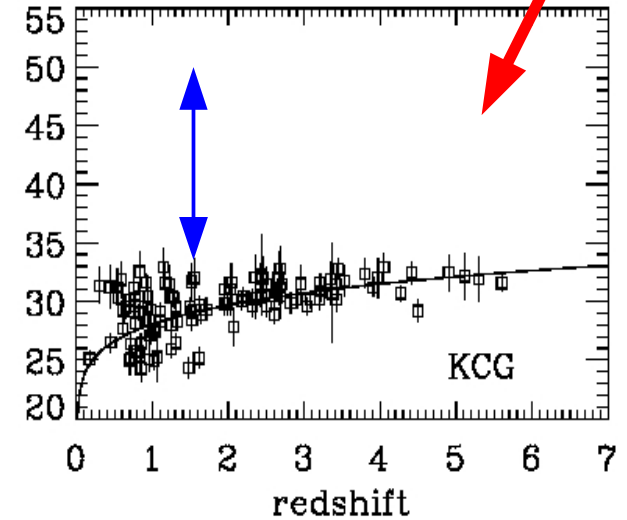
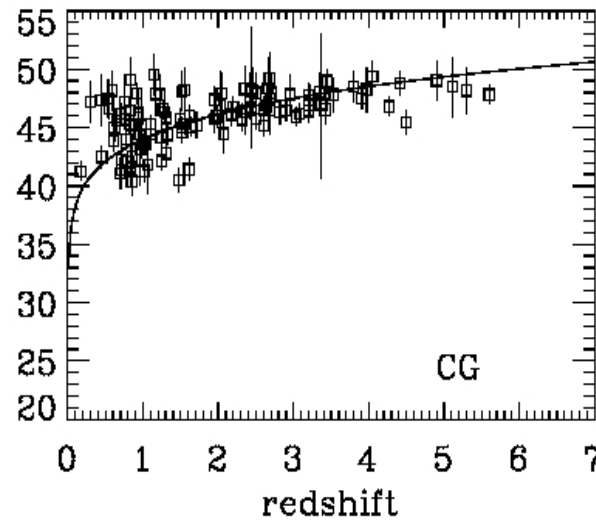
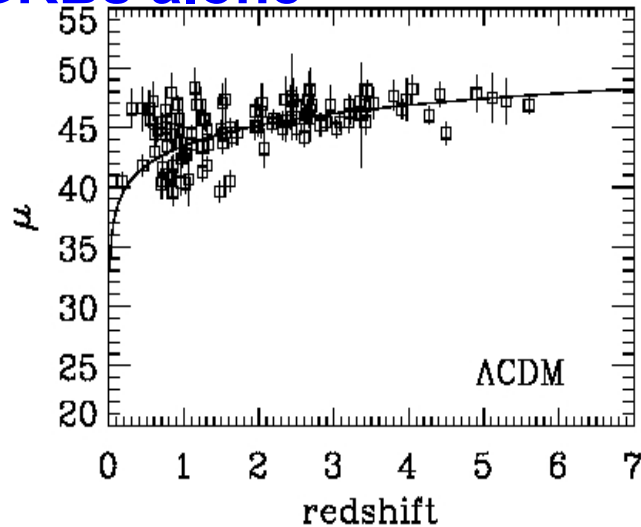
**the distance modulus μ
is indeed a model-dependent quantity**



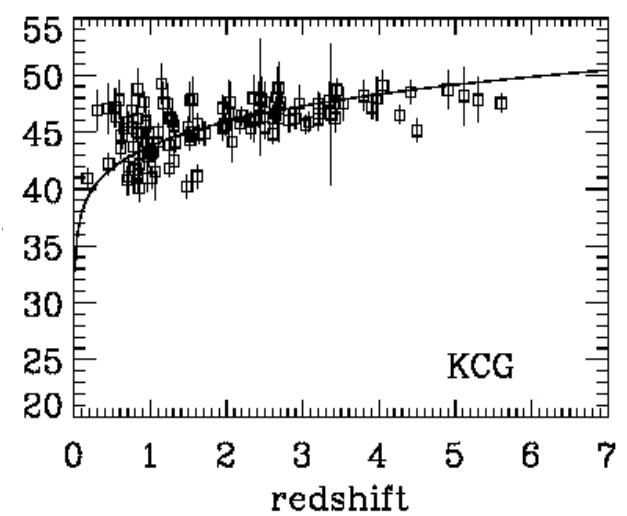
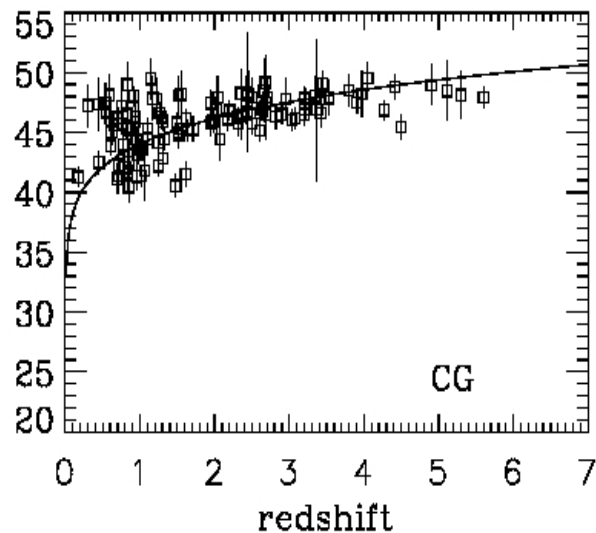
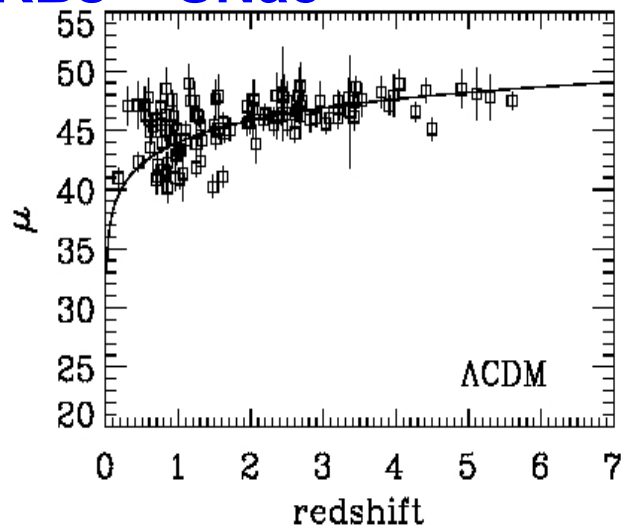
Hubble diagram of GRBs in the three models

**the distance modulus μ
is indeed a model-dependent quantity**

GRBs alone



GRBs + SNaE



Two issues:

- find the parameters that can describe the data → done
- compare the models → ?

The Bayesian Evidence

$$p(D|M) = \int p(D|\theta, M) p(\theta|M) d\theta$$

Model posterior probability

$$p(M|D) = \frac{p(D|M) p(M)}{p(D)}$$

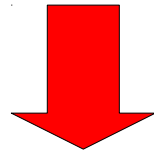
Comparing
two models:

$$\frac{p(M_1|D)}{p(M_2|D)} = \frac{p(D|M_1) p(M_1)}{p(D|M_2) p(M_2)}$$

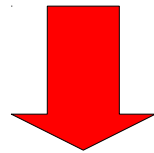
B_{12} = Bayes factor

Parallel tempering algorithm

$$p_{\beta}(\theta|D, M) = \frac{[p(D|\theta, M)]^{\beta} p(\theta|M)}{p_{\beta}(D|M)}$$



$$\frac{\partial \ln p_{\beta}(D|M)}{\partial \beta} = \langle \ln p(D|\theta, M) \rangle_{\beta}$$



$$\ln p(D|M) = \int_0^1 \langle \ln p(D|\theta, M) \rangle_{\beta} d\beta$$

20 chains (values of $\beta \in [0, 1]$)

Values of $\ln B_{12}$

M_1/M_2 sample	Λ CDM/CG	Λ CDM/KCG
GRBs	37.9	12.0
SNae	6.6	7.2
GRBs + SNae	1.5	24.3

$B_{12} > 1 \Rightarrow M_1$ favoured over M_2

Conclusions

- Λ CDM, CG, and KCG can describe the observational data
- The Bayes factor favours Λ CDM over CG and KCG

But Λ CDM has dark matter, dark energy...