#### New Results of Fully Bayesian

#### JIN XU

UCI

February 7, 2012

JIN XU New Results of Fully Bayesian

イロン イヨン イヨン イヨン

æ

#### Outline

Background Problem description Methodology Research New Results Two concerns

#### Background

Problem description Calibration Samples

#### Methodology Research

Principle Component Analysis Model Building Three source parameter sampling schemes

#### New Results

Simulation Quasar data sets

#### Two concerns

New data sets Applying wavelets to replace PCA

< 17 b

★ E → < E →</p>



- High-Energy Astrophysics
- Spectral Analysis
- Calibration Products
- Scientific Goals

イロト イヨト イヨト イヨト

æ

# High-Energy Astrophysics

- Provide understanding into high-energy regions of the Universe.
- Chandra X-ray Observatory is designed to observe X-rays from high-energy regions of the Universe.
- X-ray detectors typically count a small number of photons in each of a large number of pixels.
- Spectral Analysis aims to explore the parameterized pattern between the photon counts and energy.

・ロン ・回 と ・ ヨ と ・ ヨ と

#### An Example of One Dataset

#### TITLE = EXTENDED EMISSION AROUND A GIGAHERTZ PEAKED RADIO SOURCE DATE = 2006-12-29 T 16:10:48



JIN XU New Results of Fully Bayesian

### Calibration Uncertainty

Effective area records sensitivity as a function of energy.

**JIN XU** 

- Energy redistribution matrix can vary with energy/location.
- Point Spread Functions can vary with energy and location.





New Results of Fully Bayesian

### Incorporate Calibration Uncertainty

- Calibration Uncertainty in astronomical analysis have been generally ignored.
- No robust principled method is available.
- Our goal is to incorporate the uncertainty by Bayesian Methods.
- In this talk, we focus on uncertainty in the effective area.

**Calibration Samples** 

#### Two Main Problems

- The true effective area curve can't be observed, when we try to incorporate calibration uncertainty in estimating source parameters.
- We don't have parameterized form for effective area curve. It makes sampling hard to approach.

**Calibration Samples** 

## Generating Calibration Samples

- Drake et al. (2006), suggests to generate calibration samples of effective area curves to represent the uncertainty.
- Calibration Samples:
  {A<sub>1</sub>, A<sub>2</sub>, A<sub>3</sub>, ..., A<sub>L</sub>}



JIN XU

Principle Component Analysis Model Building Three source parameter sampling schemes

### Three Main Steps

- Use Principle Component Analysis to parameterize effective area curve.
- Model Building, that it combining source model with calibration uncertainty.
- Three source parameter sampling schemes.

イロン イヨン イヨン イヨン

Principle Component Analysis Model Building Three source parameter sampling schemes

### Use PCA to represent effective area curve

$$A = A_0 + \overline{\delta} + \sum_{j=1}^m e_j r_j v_j$$

- $A_0$  : default effective area,
  - $\overline{\delta}$  : mean deviation from  $A_0$ ,
- $r_j$  and  $v_j$ : first m principle component eigenvalues & vectors,
  - $e_i$ : independent standard normal deviations.

Capture 95% of uncertainty with m = 6 - 9.

Principle Component Analysis Model Building Three source parameter sampling schemes

#### Use PCA to represent effective area curve

PCA method has nicely parameterized effective area curve.



JIN XU New Results of Fully Bayesian

Principle Component Analysis Model Building Three source parameter sampling schemes

A simplified model of telescope response, only concerning effective area uncertainty

$$M(E;\theta) = S(E;\theta) * A(E)$$

- $M(E; \theta)$ : Observed Photon Distribution,
- $S(E; \theta)$ : True Source Model, we set it as poisson distribution with expectation equal to  $exp(-n_H * sigma(E)) * Amp * E^{(-gamma)} + bkg$ 
  - A(E): Effective Area Curve.
    - $\theta$ : source parameter,  $\theta = \{n_H, Amp, gamma, bkg\}$

Principle Component Analysis Model Building Three source parameter sampling schemes

### Scheme One: Fixed Effective Area Curved

- ▶ We assume A = A<sub>0</sub>, where A<sub>0</sub> is the default affective area curve, and may not be the true one,
- This scheme doesn't incorporate any calibration uncertainty,
- The estimation may be biased and error bars may be underestimated.
- ► Only one sampling step involved: p(θ|M, A<sub>0</sub>) ∝ L(M|θ, A<sub>0</sub>)p(A<sub>0</sub>)

Principle Component Analysis Model Building Three source parameter sampling schemes

## Scheme Two: Pragmatic Bayesian, Lee et al(2011, Apj)

- Main purpose is to reduce complexity of sampling.
- This scheme "completely" incorporates the calibration uncertainty,
- Step One: sample A from p(A)
- Step Two: sample  $\theta$  from  $p(\theta|M, A) \propto L(M|\theta, A)p(\theta)$

Principle Component Analysis Model Building Three source parameter sampling schemes

## Scheme Three: Fully Bayesian

- Use correct Bayesian Approach,
- This scheme concerns about letting the current data influence calibration products,
- Step One: sample A from  $p(A|M, \theta) \propto L(M|\theta, A)p(A)$
- Step Two: sample  $\theta$  from  $p(\theta|M, A) \propto L(M|\theta, A)p(\theta)$
- Most difficult approach to sample.

Simulation Quasar data sets

#### Eight simulated data sets

The first four data sets were all simulated without background contamination using the XSPEC model wabs\*powerlaw, nominal default effective area  $A_0$  from the calibration sample of Drake et al. (2006), and a default RMF for ACIS-S.

- Simulation 1:  $\Gamma = 2$ ,  $N_H = 2^{23} cm^{-2}$ , and  $10^5$  counts;
- Simulation 2:  $\Gamma = 1$ ,  $N_H = 2^{21} cm^{-2}$ , and  $10^5$  counts;
- Simulation 3:  $\Gamma = 2$ ,  $N_H = 2^{23} cm^{-2}$ , and  $10^4$  counts;
- Simulation 4:  $\Gamma = 1$ ,  $N_H = 2^{21} cm^{-2}$ , and  $10^4$  counts;

The other four data sets (Simulation 5-8) were generated using an extreme instance of an effective area.

・ロン ・回 と ・ ヨ と ・ ヨ と

Simulation Quasar data sets



Simulation Quasar data sets



Simulation Quasar data sets

#### Results for Simulation 3



æ

Simulation Quasar data sets



Simulation Quasar data sets



Simulation Quasar data sets



Simulation Quasar data sets

## Results for Simulation 7



æ

Simulation Quasar data sets



Simulation Quasar data sets

#### Quasar results

- 16 Quasar data sets were fit by these three models: 377, 836, 866, 1602, 3055, 3056, 3097, 3098, 3100, 3101, 3102, 3103, 3104, 3105, 3106, 3107.
- Most interesting founding for fully bayesian model is shift of parameter fitting, besides the change of standard errors.
- Both comparisons of mean and standard errors among three models are shown below.

Simulation Quasar data sets

## mean: fix-prag



JIN XU

New Results of Fully Bayesian

Simulation Quasar data sets

## mean: fix-full



JIN XU

New Results of Fully Bayesian

Simulation Quasar data sets

## mean: prag-full



JIN XU

New Results of Fully Bayesian

Simulation Quasar data sets

### sd: fix-prag



Simulation Quasar data sets

## sd: fix-full



New Results of Fully Bayesian

Simulation Quasar data sets

# sd: prag-full



Simulation Quasar data sets

#### more plots

 $\hat{\mu}_{prag}(\Gamma) = \frac{\mu_{prag}(\Gamma) - \mu_{fix}(\Gamma)}{\sigma_{fix}(\Gamma)}$ , these lines cover 2 sd.



Simulation Quasar data sets

#### more plots

 $\hat{\mu}_{full}(\Gamma) = \frac{\mu_{full}(\Gamma) - \mu_{fix}(\Gamma)}{\sigma_{fix}(\Gamma)}$ , these lines cover 2 sd.



New data sets Applying wavelets to replace PCA

#### Data set 1878

model: xsphabs.abs1\*(xsapec.kT1+xsapec.kT2)





JIN XU

New Results of Fully Bayesian

New data sets Applying wavelets to replace PCA

#### Data set 1878

model: xsphabs.abs1\*(xsapec.kT1+xsapec.kT2)

- even for fixed arf model, the results are not good;
- try to add one proportion parameter, and add data augmentation sampler to the code;
- till now, only one naive simulation has been done so far.

イロン イヨン イヨン イヨン

New data sets Applying wavelets to replace PCA

#### Discrete wavelet transformation (DWT) for quiet.arf



New data sets Applying wavelets to replace PCA

### Discrete wavelet transformation (DWT) for quiet0934.arf



New data sets Applying wavelets to replace PCA



- how to make summary of those parameters are the key point.
- future work is to sample these parameters and transform back to arf.

イロン イヨン イヨン イヨン